### 12.3 EXERCISE

## SHORT ANSWER TYPE QUESTIONS

Q1. Determine the maximum value of $\mathrm{Z}=11 x+7 y$ subject to the constraints:
$2 x+y \leq 6, x \leq 2, x \geq 0, y \geq 0$
Sol. Given that: $\mathrm{Z}=11 x+7 y$ and the constraints $2 x+y \leq 6, x \leq 2$, $x \geq 0, y \geq 0$
Let $2 x+y=6$

| $x$ | 0 | 3 |
| :--- | :--- | :--- |
| $y$ | 6 | 0 |

The shaded area OABC is the feasible region determined by the constraints

$$
2 x+y \leq 6, x \leq 2, x \geq 0, y \geq 0
$$

The feasible region is bounded.


So, maximum value will occur at a corner point of the feasible region.
Corner points are $(0,0),(2,0),(2,2)$ and $(0,6)$.
Now, evaluating the value of $Z$, we get

| Corner points | Value of $Z$ |
| :---: | :---: |
| $\mathrm{O}(0,0)$ | $11(0)+7(0)=0$ |
| $\mathrm{~A}(2,0)$ | $11(2)+7(0)=22$ |
| $\mathrm{~B}(2,2)$ | $11(2)+7(2)=36$ |
| $\mathrm{C}(0,6)$ | $11(0)+7(6)=42$ |$\leftarrow$ Maximum

Hence, the maximum value of Z is 42 at $(0,6)$.
Q2. Maximise $\mathrm{Z}=3 x+4 y$, subject to the constraints: $x+y \leq 1, x \geq 0$, $y \geq 0$.
Sol. Given that: $\mathrm{Z}=3 x+4 y$ and the constraints $x+y \leq 1, x \geq 0, y \geq 0$
Let
$x+y=1$

| $x$ | 1 | 0 |
| :--- | :--- | :--- |
| $y$ | 0 | 1 |

The shaded area $O A B$ is the feasible region determined by $x+y \leq 1, x \geq 0, y \geq 0$.
The feasible region is bounded. So, maximum value will occur at the corner points $\mathrm{O}(0,0)$, $\mathrm{A}(1,0), \mathrm{B}(0,1)$.
Now, evaluating the value of Z , we get


| Corner points | Value of $Z$ |
| :---: | :---: |
| $\mathrm{O}(0,0)$ | $3(0)+4(0)=0$ |
| $\mathrm{~A}(1,0)$ | $3(1)+4(0)=3$ |
| $\mathrm{~B}(0,1)$ | $3(0)+4(1)=4$ |$\leftarrow$ Maximum

Hence, the maximum value of Z is 4 at $(0,1)$.
Q3. Maximise the function $\mathrm{Z}=11 x+7 y$ subject to the constraints: $x \leq 3, y \leq 2, x \geq 0, y \geq 0$.
Sol. The shaded region is the feasible region determined by the constraints $x \leq 3, y \leq 2$, $x \geq 0, y \geq 0$.
The feasible region is bounded with four corners $\mathrm{O}(0,0), \mathrm{A}(3,0), \mathrm{B}(3,2)$ and $\mathrm{C}(0,2)$.
So, the maximum value can
 occur at any corner.
Let us evaluate the value of Z .

| Corner points | Value of $Z$ |
| :---: | :---: |
| $\mathrm{O}(0,0)$ | $11(0)+7(0)=0$ |
| $\mathrm{~A}(3,0)$ | $11(3)+7(0)=33$ |
| $\mathrm{~B}(3,2)$ | $11(3)+7(2)=47$ |
| $\mathrm{C}(0,2)$ | $11(0)+7(2)=14$ |

Hence, the maximum value of the function $Z$ is 47 at $(3,2)$.
Q4. Minimise $\mathrm{Z}=13 x-15 y$ subject to the constraints:
$x+y \leq 7,2 x-3 y+6 \geq 0, x \geq 0, y \geq 0$.
Sol. Given that: $\mathrm{Z}=13 x-15 y$ and the constraints
$x+y \leq 7,2 x-3 y+6 \geq 0, x \geq 0, y \geq 0$

Let $x+y=7$

| $x$ | 3 | 4 |
| :---: | :---: | :---: |
| $y$ | 4 | 3 |

Let $2 x-3 y+6=0$

| $x$ | 1 | -3 |
| :---: | :---: | :---: |
| $y$ | 2 | 0 |

The shaded region is the feasible region determined

by the constraints $x+y \leq 7,2 x-3 y+6 \geq 0, x \geq 0, y \geq 0$
The feasible region is bounded with four corners
$\mathrm{O}(0,0), \mathrm{A}(7,0), \mathrm{B}(3,4), \mathrm{C}(0,2)$
So, the maximum value can occur at any corner.
Let us evaluate the value of Z .

| Corner points | Value of $Z$ |
| :---: | :---: |
| $\mathrm{O}(0,0)$ | $13(0)-15(0)=0$ |
| $\mathrm{~A}(7,0)$ | $13(7)-15(0)=91$ |
| $\mathrm{~B}(3,4)$ | $13(3)-15(4)=-21$ |
| $\mathrm{C}(0,2)$ | $13(0)-15(2)=-30$ |$\leftarrow$ Minimum

Hence, the minimum value of Z is -30 at $(0,2)$.
Q5. Determine the maximum value of $Z=3 x+4 y$ if the feasible region (shaded) for a LPP is shown in figure.
Sol. As shown in the figure, OAED is the feasible region.
At A, $y=0 \therefore 2 x+y=104$
$\Rightarrow x=52$
Which gives corner point A $=(52,0)$
At D, $x=0 \therefore x+2 y=76 \Rightarrow y=38$


Which gives corner point $\mathrm{D}=(0,38)$
Now solving the given equations, we get

| $x+2 y$ | $=$ |
| ---: | :--- |
| $26+y$ | $=104$ |
| $2 x+4 y$ | $=152$ |
| $2 x+y$ | $=$ |
| $(-)$ |  |
| $(-) \quad(-)$ | $(-)$ |

$$
\begin{aligned}
& & x+2(16) & =76 \\
\Rightarrow & & x & =76-32=44
\end{aligned}
$$

So, the corner point $\mathrm{E}=(44,16)$
Evaluating the maximum value of $Z$, we get

| Corner points | $Z=3 x+4 y$ |
| :---: | :---: |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=3(0)+4(0)=0$ |
| $\mathrm{~A}(52,0)$ | $\mathrm{Z}=3(52)+4(0)=156$ |
| $\mathrm{E}(44,16)$ | $\mathrm{Z}=3(44)+4(16)=196$ |
| $\mathrm{D}(0,38)$ | $\mathrm{Z}=3(0)+4(38)=152$ |

Hence, the maximum value of Z is 196 at $(44,16)$.
Q6. Feasible region (shaded) for a LPP is shown in figure. Maximise $Z=5 x+7 y$.
Sol. OABC is the feasible region whose corner points are $\mathrm{O}(0,0), \mathrm{A}(7,0), \mathrm{B}(3,4)$ and C $(0,2)$
Evaluating the value of $Z$, we get


Hence, the maximum value of Z is 43 at $(3,4)$.
Q7. The feasible region for a LPP is shown in figure. Find the minimum value of $Z=11 x+7 y$.
Sol. As per the given figure, ABCA is the feasible region. Corner points $C(0,3), B(0,5)$ and for $A$, we have to solve equations

$$
x+3 y=9
$$

and $\quad x+y=5$
Which gives $x=3, y=2$
i.e., $A(3,2)$


Evaluating the value of Z , we get

| Corner points | Value of Z |
| :---: | :---: |
| $\mathrm{A}(3,2)$ | $\mathrm{Z}=11(3)+7(2)=47$ |
| $\mathrm{~B}(0,5)$ | $\mathrm{Z}=11(0)+7(5)=35$ |
| $\mathrm{C}(0,3)$ | $\mathrm{Z}=11(0)+7(3)=21$ |$\leftarrow$ Minimum

Hence, the minimum value of Z is 21 at $(0,3)$.
Q8. Refer to Exercise 7 above. Find the maximum value of Z .
Sol. As per the evaluating table for the value of $Z$, it is clear that the maximum value of Z is 47 at $(3,2)$.
Q9. The feasible region for a LPP is shown in figure. Evaluate $\mathrm{Z}=4 x+y$ at each of the corner points of this region. Find the minimum value of $Z$, if it exists.
Sol. As per the given figure, ABC is the feasible region which is open unbounded.
Here, we have

$$
\begin{equation*}
x+y=3 \tag{i}
\end{equation*}
$$

and $x+2 y=4$
$Z=4 x+y$
Solving eq. (i) and (ii), we get
$x=2$ and $y=1$
So, the corner points are $\mathrm{A}(4,0), \mathrm{B}(2,1)$ and $\mathrm{C}(0,3)$


Let us evaluate the value of $Z$

| Corner points | $\mathrm{Z}=4 x+y$ |
| :---: | :---: |
| $\mathrm{~A}(4,0)$ | $\mathrm{Z}=4(4)+(0)=16$ |
| $\mathrm{~B}(2,1)$ | $\mathrm{Z}=4(2)+(1)=9$ |
| $\mathrm{C}(0,3)$ | $\mathrm{Z}=4(0)+(3)=3$ |$\leftarrow$ Minimum

Now, the minimum value of $Z$ is 3 at $(0,3)$ but since, the feasible region is open bounded so it may or may not be the minimum value of $Z$.
Therefore, to face such situation, we draw a graph of $4 x+y<3$ and check whether the resulting open half plane has no point in common with feasible region. Otherwise Z will have no minimum value. From the graph, we conclude that there is no common point with the feasible region.
Hence, $Z$ has the minimum value 3 at ( 0,3 ).
Q10. In given figure, the feasible region (shaded) for a LPP is shown. Determine the maximum and minimum value of $\mathrm{Z}=x+2 y$.


Sol. Here, corner points are given as follows:
$\mathrm{R}\left(\frac{7}{2}, \frac{3}{4}\right), \mathrm{Q}\left(\frac{3}{2}, \frac{15}{4}\right), \mathrm{P}\left(\frac{3}{13}, \frac{24}{13}\right)$ and $\mathrm{S}\left(\frac{18}{7}, \frac{2}{7}\right)$.
Now, evaluating the value of $Z$ for the feasible region RQPS.

| Corner points | Value of $Z=x+2 y$ |
| :---: | :---: |
| $\mathrm{R}\left(\frac{7}{2}, \frac{3}{4}\right)$ | $Z=\frac{7}{2}+2\left(\frac{3}{4}\right)=5$ |
| $\mathrm{Q}\left(\frac{3}{2}, \frac{15}{4}\right)$ | $Z=\frac{3}{2}+2\left(\frac{15}{4}\right)=9$ |
| $\mathrm{P}\left(\frac{3}{13}, \frac{24}{13}\right)$ | $Z=\frac{3}{13}+2\left(\frac{24}{13}\right)=\frac{51}{13}$ |
| $\mathrm{~S}\left(\frac{18}{7}, \frac{2}{7}\right)$ | $Z=\frac{18}{7}+2\left(\frac{2}{7}\right)=\frac{22}{7}$ |$\leftarrow$ Maximum

Hence, the maximum value of $Z$ is 9 at $\left(\frac{3}{2}, \frac{15}{4}\right)$ and the minimum value of $Z$ is $\frac{22}{7}$ at $\left(\frac{18}{7}, \frac{2}{7}\right)$.
Q11. A manufacturer of electric circuits has a stock of 200 resistors, 120 transistors and 150 capacitors and is required to produce
two types of circuits A and B. Type A requires 20 resistors, 10 transistors and 10 capacitors. Type B requires 10 resistors, 20 transistors and 30 capacitors. If the profit on type A circuit is ₹ 50 and that on type B circuit is ₹ 60 , formulate this problem as a LPP so that the manufacturer can maximise his profit.
Sol. Let $x$ units of type A and $y$ units of type $B$ electric circuits be produced by the manufacturer.
As per the given information, we construct the following table:

| Items | Type $A(x)$ | Type B (y) | Maximum stock |
| :--- | :---: | :---: | :---: |
| Resistors | 20 | 10 | 200 |
| Transistors | 10 | 20 | 120 |
| Capacitors | 10 | 30 | 150 |
| Profit | $₹ 50$ | $₹ 60$ | $\mathrm{Z}=50 x+60 y$ |

Now, we have the total profit in rupees $Z=50 x+60 y$ to maximise subject to the constraints
$20 x+10 y \leq 200$
...(i);
$10 x+20 y \leq 120$
$10 x+30 y \leq 150$
...(iii);
$x \geq 0, y \geq 0$

Hence, the required LPP is
Maximise $\mathrm{Z}=50 x+60 y$ subject to the constraints
$20 x+10 y \leq 200 \Rightarrow 2 x+y \leq 20 ; 10 x+20 y \leq 120 \Rightarrow x+2 y \leq 12$
and $\quad 10 x+30 y \leq 150 \Rightarrow x+3 y \leq 15, x \geq 0, y \geq 0$
Q12. A firm has to transport 1200 packages using large vans which can carry 200 packages each and small vans which can take 80 packages each. The cost for engaging each large van is ₹ 400 and each small van is ₹ 200 . Not more than ₹ 3000 is to be spent on the job and the number of large vans cannot exceed the number of small vans. Formulate this problem as a LPP given that the objective is to minimise cost.
Sol. Let $x$ and $y$ be the number of large and small vans respectively. From the given information, we construct the following corresponding constraints table;

| Items | Large vans <br> $(x)$ | Small vans <br> $(y)$ | Maximum/ <br> Minimum |
| :--- | :---: | :---: | :---: |
| Packages | 200 | 80 | 1200 |
| Cost | 400 | 200 | 3000 |

Now the objective function for minimum cost is

$$
Z=400 x+200 y
$$

Subject to the constraints;

$$
\begin{equation*}
200 x+80 y \geq 1200 \Rightarrow 5 x+2 y \geq 30 \tag{i}
\end{equation*}
$$

$$
\begin{align*}
& 400 x+200 y & \leq 3000 \Rightarrow 2 x+y \leq 15 & \ldots(i i)  \tag{ii}\\
& x & \Rightarrow y &  \tag{iii}\\
\text { and } & x & \geq 0, y \geq 0 & \text { (non-negative constraints) }
\end{align*}
$$

Hence, the required LPP is to minimise $Z=400 x+200 y$
Subject to the constraints $5 x+2 y \geq 30,2 x+y \leq 15, x \leq y$ and $x \geq 0, y \geq 0$.
Q13. A company manufactures two types of screws A and B. All the screws have to pass through a threading machine and a slotting machine. A box of type A screws requires 2 minutes on the threading machine and 3 minutes on the slotting machine. A box of type B screws requires 8 minutes of threading on threading machine and 2 minutes on the slotting machine. In a week, each machine is available for 60 hours.
On selling these screws, the company gets a profit of ₹ 100 per box on type A screws and ₹ 170 per box on type B screws. Formulate this problem as a LPP given that the objective is to maximise profit.
Sol. Let the company manufactures $x$ boxes of type A screws and $y$ boxes of type B screws.
From the given information, we can construct the following table.

| Items | Type A <br> $(x)$ | Type B <br> $(y)$ | Minimum time available <br> on each machine <br> in a week |
| :--- | :---: | :---: | :---: |
| Time required on <br> threading machine | 2 | 8 | $60 \times 60=3600$ minutes |
| Time required on <br> slotting machine | 3 | 2 | $60 \times 60=3600$ minutes |
| Profit | $₹ 100$ | $₹ 170$ |  |

As per the information in the above table, the objective function for maximum profit $Z=100 x+170 y$
Subject to the constraints

$$
\begin{align*}
2 x+8 y & \leq 3600 \quad  \tag{i}\\
3 x+2 y & \leq 3600  \tag{ii}\\
x & \geq 0, y \geq 0
\end{align*} \quad \text { (non-negative constraints) }
$$

Hence, the required LPP is
Maximise $\quad Z=100 x+170 y$
Subject to the constraints,
$x+4 y \leq 1800,3 x+2 y \leq 3600, x \geq 0, y \geq 0$.
Q14. A company manufactures two types of sweaters: type A and type B. It costs ₹ 360 to make a type A sweater and ₹ 120 to make a type B sweater. The company can make at most 300 sweaters and spend at most ₹ 72000 a day. The number of sweaters of
type B cannot exceed the number of sweaters of type A by more than 100. The company makes a profit of ₹ 200 for each sweater of type A and ₹ 120 for every sweater of type B.
Formulate this problem at a LPP to maximise the profit to the company.
Sol. Let $x$ and $y$ be the number of sweaters of type A and type B respectively.
From the given information, we have the following constraints.
$360 x+120 y \leq 72000 \Rightarrow 3 x+y \leq 600$
$x+y \leq 300 \quad$...(ii); $x+100 \geq y \Rightarrow y \leq x+100$
Profit (Z) $=200 x+120 y$
Hence, the required LPP to maximise the profit is
Maximise $\mathrm{Z}=200 x+120 y$ subject to the constraints
$3 x+y \leq 600, x+y \leq 300, y \leq x+100, x \geq 0, y \geq 0$.
Q15. A man rides his motorcycle at the speed of $50 \mathrm{~km} / \mathrm{hr}$. He has to spend ₹ 2 per km on petrol. If he rides it at a faster speed of 80 $\mathrm{km} / \mathrm{hr}$, the petrol cost increases to ₹ 3 per km. He has atmost $₹ 120$ to spend on petrol and one hour's time. He wishes to find the maximum distance that he can travel.
Express this problem as a linear programming problem.
Sol. Let the man covers $x \mathrm{~km}$ on his motorcycle at the speed of $50 \mathrm{~km} / \mathrm{hr}$ and covers $y \mathrm{~km}$ at the speed of $80 \mathrm{~km} / \mathrm{hr}$.
So, cost of petrol $=2 x+3 y$
The man has to spend ₹ 120 atmost on petrol
$\therefore \quad 2 x+3 y \leq 120$
Now, the man has only 1 hr time

$$
\begin{align*}
\therefore \quad \frac{x}{50}+\frac{y}{80} & \leq 1 \Rightarrow 8 x+5 y \leq 400  \tag{ii}\\
x & \geq 0, y \geq 0
\end{align*}
$$

To have maximum distance $\mathrm{Z}=x+y$.
Hence, the required LPP to travel maximum distance is maximise $\mathrm{Z}=x+y$, subject to the constraints
$2 x+3 y \leq 120,8 x+5 y \leq 400, x \geq 0, y \geq 0$.

## LONG ANSWER TYPE QUESTIONS

Q16. Refer to Exercise 11. How many of circuits of Type A and of Type B, should be produced by the manufacturer so as to maximise his profit? Determine the maximum profit.
Sol. As per the solution of Question No. 11, we have Maximise $Z=50 x+60 y$ subject to the contraints $2 x+y \leq 20 \ldots(i) ; x+2 y \leq 12 \ldots$..(ii); $x+3 y \leq 15 \ldots$..(iii); $x \geq 0, y \geq 0 \ldots$ (iv)
Let us draw the table for the above statements
Table for ( $i$ )

| $x$ | 0 | 10 |
| ---: | ---: | ---: |
| $y$ | 20 | 0 |$;$

Table for (ii)

| $x$ | 0 | 12 |
| ---: | ---: | ---: |
| $y$ | 6 | 0 |

Table for (ii)

| $x$ | 0 | 15 |
| ---: | ---: | ---: |
| $y$ | 5 | 0 |



Solving eq. (i) and (ii) we get,
$x=\frac{28}{3}, y=\frac{4}{3} \quad \therefore \mathrm{~B}\left(\frac{28}{3}, \frac{4}{3}\right)$ is the corner
Solving eq. (ii) and (iii) we get,
$x=6, y=3 \quad \therefore \mathrm{C}(6,3)$ is the corner
Solving eq. (i) and (iii) we get,
$x=9, y=2 \quad$ (not included in the feasible region)
Here, OABCD is the feasible region.
So, the corner points are $\mathrm{O}(0,0), \mathrm{A}(10,0), \mathrm{B}\left(\frac{28}{3}, \frac{4}{3}\right), \mathrm{C}(6,3)$ and $\mathrm{D}(0,5)$.
Let us evaluate the value of Z

| Corner points | Corresponding values of $Z=50 x+60 y$ |
| :---: | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=50(0)+60(0)=0$ |
| $\mathrm{~A}(10,0)$ | $\mathrm{Z}=50(10)+60(0)=500$ |
| $\mathrm{~B}\left(\frac{28}{3}, \frac{4}{3}\right)$ | $\mathrm{Z}=50\left(\frac{28}{3}\right)+60\left(\frac{4}{3}\right)=\frac{1400}{3}+\frac{240}{3}$ <br>  <br> $=\frac{1640}{3}=546.6$ |
| $\mathrm{C}(6,3)$ | $\mathrm{Z}=50(6)+60(3)=480$ |
| $\mathrm{D}(0,5)$ | $\mathrm{Z}=50(0)+60(5)=300$ |

Here, the maximum profit is ₹ 546.6 which is not possible for number of items in fraction.

Hence, the maximum profit for the manufacturer is ₹ 480 at $(6,3)$. Type $A=6$ and Type $B=3$.
Q17. Refer to Exercise 12. What will be the minimum cost?
Sol. As per the solution of Q. 12., we have $Z=400 x+200 y$ Subject to the constraints
$5 x+2 y \geq 30$
...(i); $2 x+y \leq 15$
$x \leq y, x \geq 0, y \geq 0$
$x-y \leq 0$
Let $5 x+2 y=30$

| $x$ | 0 | 6 |
| :---: | :---: | :---: |
| $y$ | 15 | 0 |

Let $2 x+y=15$

| $x$ | 0 | 7.5 |
| :---: | :---: | :---: |
| $y$ | 15 | 0 |

Let $x-y=0$

| $x$ | 0 | 1 |
| :--- | :--- | :--- |
| $y$ | 0 | 1 |



Solving eq. (i) and (iii) we get; $x=\frac{30}{7}$ and $y=\frac{30}{7}$ and on solving eq. (ii) and (iii) we get, $x=5$ and $y=5$
Here, ABC is the shaded feasible region whose corner points are $A\left(\frac{30}{7}, \frac{30}{7}\right), B(5,5)$ and $C(0,15)$
Evaluating the value of $Z$, we have

| Corner points | Value of $\mathrm{Z}=400 x+200 y$ |
| :--- | :--- |
| $\mathrm{~A}\left(\frac{30}{7}, \frac{30}{7}\right)$ | $\mathrm{Z}=400\left(\frac{30}{7}\right)+200\left(\frac{30}{7}\right)$  <br>  $=\frac{18000}{7}=2571.4$ |
| $\mathrm{~B}(5,5)$ | $\mathrm{Z}=400(5)+200(5)=3000$ |
| $\mathrm{C}(0,15)$ | $\mathrm{Z}=400(0)+200(15)=3000$ |

Hence, the required minimum cost is ₹ 2571.4 at $\left(\frac{30}{7}, \frac{30}{7}\right)$.
Q18. Refer to Exercise 13. Solve the linear programming program and determine the maximum profit to the manufacturer.
Sol. As per the solution
of Q. 13 , we have:

Let $3 x+2 y=3600$

| $x$ | 0 | 1200 |
| :---: | :---: | :---: |
| $y$ | 1800 | 0 |

Let $x+4 y=1800$

| $x$ | 0 | 1800 |
| :---: | :---: | :---: |
| $y$ | 450 | 0 |



Maximise $Z=100 x+170 y$ subject to the constraints

$$
\begin{equation*}
3 x+2 y \leq 3600 \quad \ldots(i) ; x+4 y \leq 1800 \tag{ii}
\end{equation*}
$$

On solving eq. (i) and (ii) we get
$x=1080$ and $y=180$
OABC is the feasible region whose corner points are $\mathrm{O}(0,0)$, A(1200, 0), B(1080, 180), C(0, 450).
Let us evaluate the value of $Z$.

| Corner points | Value of $\mathrm{Z}=100 x+170 y$ |
| :---: | :---: |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=100(0)+170(0)=0$ |
| $\mathrm{~A}(1200,0)$ | $\mathrm{Z}=100(1200)+0=120000$ |
| $\mathrm{~B}(1080,180)$ | $\mathrm{Z}=100(1080)+170(180)$ <br> $=138600$ |
| $\mathrm{C}(0,450)$ | $\mathrm{Z}=170(450)=76500$ |$\leftarrow$ Maximum

Hence, the maximum value of Z is 138600 at $(1080,180)$.
Q19. Refer to Exercise 14. How many sweaters of each type should the company make in a day so as to get a maximum profit? What is the maximum profit?
Sol. Referring to the solution of Q. 14, we have
Maximise

$$
Z=200 x+120 y \text { subject to the constraints }
$$

$$
\begin{align*}
x+y & \leq 300 \quad \ldots(i) ; \quad 3 x+y \leq 600  \tag{ii}\\
x-y & \geq-100  \tag{iii}\\
x & \geq 0, y \geq 0
\end{align*}
$$

On solving eq. (i) and (iii) we have $x=100, y=200$
On solving eq. (i) and (ii) we get
$x=150, y=150$
Let $x+y=300$

$$
\text { Let } 3 x+y=600
$$

Let $x+y=-100$

| $x$ | 0 | 300 |
| :---: | :---: | :---: |
| $y$ | 300 | 0 |


| $x$ | 0 | 200 |
| :---: | :---: | :---: |
| $y$ | 600 | 0 |


| $x$ | 0 | -100 |
| :---: | :---: | :---: |
| $y$ | 100 | 0 |



Here, the shaded region is the feasible region whose corner points are $\mathrm{O}(0,0), \mathrm{A}(200,0), \mathrm{B}(150,150), \mathrm{C}(100,200), \mathrm{D}(0,100)$. Let us evaluate the value of $Z$.

| Corner points | Value of $Z=200 x+120 y$ |
| :--- | :--- |
| $\mathrm{O}(0,0)$ | $Z=200(0)+120(0)=0$ |
| $\mathrm{~A}(200,0)$ | $\mathrm{Z}=200(200)+120(0)=40000$ |
| $\mathrm{~B}(150,150)$ | $\mathrm{Z}=200(150)+120(150)=48000$ |
| $\mathrm{C}(100,200)$ | $\mathrm{Z}=200(100)+120(200)=44000$ |
| $\mathrm{D}(0,100)$ | $\mathrm{Z}=200(0)+120(100)=12000$ |

Hence, the maximum value of $Z$ is 48000 at $(150,150)$ i.e., 150 sweaters of each type.
Q20. Refer to Exercise 15, Determine the maximum distance that the man can travel.
Sol. Referring to the solution of Q. 15 , we have
Maximise $\mathrm{Z}=x+y$ subject to the constraints
Let $2 x+3 y=120$
Let $8 x+5 y=400$

| $x$ | 0 | 60 |
| :---: | :---: | :---: |
| $y$ | 40 | 0 |


| $x$ | 0 | 50 |
| :---: | :---: | :---: |
| $y$ | 80 | 0 |



$$
\begin{aligned}
2 x+3 y & \leq 120 \ldots(i) ; 8 x+5 y \leq 400 \\
x & \geq 0, y \geq 0
\end{aligned}
$$

On solving eq. (i) and (ii) we get; $x=\frac{300}{7}$ and $y=\frac{80}{7}$
Here, OABC is the feasible region whose corner points are $\mathrm{O}(0,0), \mathrm{A}(50,0), \mathrm{B}\left(\frac{300}{7}, \frac{80}{7}\right)$ and $\mathrm{C}(0,40)$.
Let us evaluate the value of $Z$

| Corner points | Value of $\mathrm{Z}=x+y$ |
| :--- | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=0+0=0$ |
| $\mathrm{~A}(50,0)$ | $\mathrm{Z}=50+0=50 \mathrm{~km}$ |
| $\mathrm{~B}\left(\frac{300}{7}, \frac{80}{7}\right)$ | $\mathrm{Z}=\frac{300}{7}+\frac{80}{7}=\frac{380}{7}=54.3 \mathrm{~km}$ |
| $\mathrm{C}(0,40)$ | $\mathrm{Z}=0+40=40 \mathrm{~km}$ |

Hence, the maximum distance that the man can travel is $54 \frac{2}{7} \mathrm{~km}$ at $\left(\frac{300}{7}, \frac{80}{7}\right)$.
Q21. Maximise $Z=x+y$ subject to $x+4 y \leq 8,2 x+3 y \leq 12,3 x+y \leq 9$, $x \geq 0, y \geq 0$.
Sol. We are given that $\mathrm{Z}=x+y$ subject to the constraints

$$
\begin{gathered}
x+4 y \leq 8 \\
2 x+3 y \leq 12
\end{gathered}
$$

$$
3 x+y \leq 9
$$

$$
x \geq 0, y \geq 0
$$

| $x$ | 0 | 8 |
| :--- | :--- | :--- |
| $y$ | 2 | 0 |


| $x$ | 0 | 6 |
| :--- | :--- | :--- |
| $y$ | 4 | 0 |


| $x$ | 0 | 3 |
| :---: | :---: | :---: |
| $y$ | 9 | 0 |



On solving eq. (i) and (iii) we get
$x=\frac{28}{11}$ and $y=\frac{15}{11}$
Here, OABC is the feasible region whose corner points are
$\mathrm{O}(0,0), \mathrm{A}(3,0), \mathrm{B}\left(\frac{28}{11}, \frac{15}{11}\right), \mathrm{C}(0,2)$
Let us evaluate the value of $Z$

| Corner points | Value of $\mathrm{Z}=x+y$ |
| :--- | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=0+0=0$ |
| $\mathrm{~A}(3,0)$ | $\mathrm{Z}=3+0=3$ |
| $\mathrm{~B}\left(\frac{28}{11}, \frac{15}{11}\right)$ | $\mathrm{Z}=\frac{28}{11}+\frac{15}{11}=\frac{43}{11}=3.9$ |
| $\mathrm{C}(0,2)$ | $\mathrm{Z}=0+2=2$ |$\leftarrow$ Maximum

Hence, the maximum value of Z is 3.9 at $\left(\frac{28}{11}, \frac{15}{11}\right)$.
Q22. A manufacturer produces two Models of bikes-Model X and Model Y. Model X takes a 6 man-hours to make per unit, while Model Y takes 10 man-hours per unit. There is a total of 450 man-hour available per week. Handling and marketing costs are $₹ 2,000$ and $₹ 1,000$ per unit for Models $X$ and $Y$ respectively. The total funds available for these purposes are $₹ 80,000$ per week. Profits per unit for Models X and Y are $₹ 1,000$ and $₹ 500$ respectively. How many bikes of each model should the manufacturer produce so as to yield a maximum profit? Find the maximum profit.
Sol. Let $x$ and $y$ be the number of Models of bike produced by the manufacturer.
Given information is
Model $X$ takes 6 man-hours to make per unit
Model Y takes 10 man-hours to make per unit
Total man-hours available $=450$
$\therefore \quad 6 x+10 y \leq 450 \Rightarrow 3 x+5 y \leq 225$
Handling and marketing cost of Model X and Y are $₹ 2,000$ and ₹ 1,000 respectively
Total funds available is ₹ 80,000 per week

$$
\begin{array}{rlrl}
\therefore & 2000 x+1000 y & \leq 80,000 \\
\Rightarrow & & 2 x+y & \leq 80 \tag{ii}
\end{array}
$$

and

$$
x \geq 80, y \geq 0
$$

Profit (Z) per unit of models $X$ and $Y$ are $₹ 1,000$ and $₹ 500$ respectively
So, $\quad Z=1000 x+500 y$
The required LPP is
Maximise $Z=1000 x+500 y$ subject to the constraints

$$
\begin{equation*}
3 x+5 y \leq 225 \tag{i}
\end{equation*}
$$

| $x$ | 0 | 75 |
| :---: | :---: | :---: |
| $y$ | 45 | 0 |

$$
\begin{equation*}
2 x+y \leq 80 \tag{ii}
\end{equation*}
$$

| $x$ | 0 | 40 |
| :---: | :---: | :---: |
| $y$ | 80 | 0 |

$$
\begin{equation*}
x \geq 0, y \geq 0 \tag{iii}
\end{equation*}
$$

On solving eq. (i) and (ii) we get, $x=25, y=30$ Here, the feasible region $\mathbf{V}$ is OABC , whose corner points are
$\mathrm{O}(0,0), \mathrm{A}(40,0), \mathrm{B}(25,30)$ and $C(0,45)$.
Let us evaluate the value of Z .

$(0,0)$


| Corner points | Value of $\mathrm{Z}=1000 x+500 y$ |
| :---: | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=0+0=0$ |
| $\mathrm{~A}(40,0)$ | $\mathrm{Z}=1000(40)+0=40,000$ |
| $\mathrm{~B}(25,30)$ | $\mathrm{Z}=1000(25)+500(30)=40,000$ |
| $\mathrm{C}(0,45)$ | $\mathrm{Z}=0+500(45)=22500$ |
| $\leftarrow$ | $\leftarrow$ Maximum |

Hence, the maximum profit is ₹ 40,000 by producing 25 bikes of Model X and 30 bikes of Model Y.

Q23. In order to supplement daily diet, a person wishes to take some $X$ and some wishes $Y$ tablets. The contents of iron, calcium and vitamins in $X$ and $Y$ (in milligram per tablet) are given as below:

| Tablets | Iron | Calcium | Vitamin |
| :---: | :---: | :---: | :---: |
| X | 6 | 3 | 2 |
| Y | 2 | 3 | 4 |

The person needs atleast 18 milligrams of iron, 21 milligrams of calcium and 16 milligrams of vitamin. The price of each tablet of $X$ and $Y$ is $₹ 2$ and $₹ 1$ respectively. How many tablets of each should the person take in order to satisfy the above requirement at the minimum cost?
Sol. Let there be $x$ units of tablet $X$ and $y$ units of tablet $Y$ So, according to the given information, we have

$$
\begin{align*}
6 x+2 y \geq 18 & \Rightarrow \quad 3 x+y \geq 9  \tag{i}\\
3 x+3 y \geq 21 & \Rightarrow \quad x+y \geq 7  \tag{ii}\\
2 x+4 y \geq 16 & \Rightarrow \quad x+2 y \geq 8  \tag{iii}\\
x \geq 0, y & \geq 0 \tag{iv}
\end{align*}
$$

| $x$ | 0 | 3 |
| :--- | :--- | :--- |
| $y$ | 9 | 0 |


| $x$ | 0 | 7 |
| :---: | :---: | :---: |
| $y$ | 7 | 0 |
| $x$ | 0 | 8 |
| $y$ | 4 | 0 |

The price of each table of $X$ type is $₹ 2$ and that of $y$ is $₹ 1$. So, the required LPP is
Minimise $\mathrm{Z}=2 x+y$ subject to the constraints $3 x+y \geq 9, x+y \geq 7, x+2 y \geq 8, x \geq 0, y \geq 0$


On solving (ii) and (iii) we get
$x=6$ and $y=1$

On solving $(i)$ and (ii) we get $x=1$ and $y=6$
From the graph, we see that the feasible region $A B C D$ is unbounded whose corner points are $A(8,0), B(6,1), C(1,6)$ and $\mathrm{D}(0,9)$.
Let us evaluate the value of $Z$

| Corner points | Value of $\mathrm{Z}=2 x+y$ |
| :---: | :--- |
| $\mathrm{~A}(8,0)$ | $\mathrm{Z}=2(8)+0=16$ |
| $\mathrm{~B}(6,1)$ | $\mathrm{Z}=2(6)+1=13$ |
| $\mathrm{C}(1,6)$ | $\mathrm{Z}=2(1)+6=8$ |
| $\mathrm{D}(0,9)$ | $\mathrm{Z}=2(0)+9=9$ |$\leftarrow$ Minimum

Here, we see that 8 is the minimum value of $Z$ at $(1,6)$ but the feasible region is unbounded. So, 8 may or may not be the minimum value of $Z$.
To confirm it, we will draw a graph of inequality $2 x+y<8$ and check if it has a common point.
We see from the graph that there is no common point on the line.
Hence, the minimum value of Z is 8 at $(1,6)$.
Tablet $\mathrm{X}=1$
Table $\mathrm{Y}=6$.
Q24 A company makes 3 models of calculators: A, B and C at factory I and factory II. The company has orders for atleast 6400 calculators of model A, 4000 calculators of model B and 4800 calculators of model C. At factory I, 50 calculators of model A, 50 of model B and 30 of model C are made everyday; at factory II, 40 calculators of model A, 20 of model B and 40 of model C are made everyday. It costs $₹ 12,000$ and $₹ 15000$ each day to operate factory I and II respectively. Find the number of days each factory should operate to minimise the operating costs and still meet the demand.
Sol. Let factory I be operated for $x$ days and II for $y$ days
At factory I: 50 calculators of model A and at factory II, 40 calculators of model A are made everyday.
Company has orders of atleast 6400 calculators of model A.
$\therefore 50 x+40 y \geq 6400 \Rightarrow 5 x+4 y \geq 640$
Also, at factory I, 50 calculators of model B and at factory II, 20 calculators of model B are made everyday.
Company has the orders of atleast 4000 of calculators of model B.
$\therefore 50 x+20 y \geq 4000 \Rightarrow 5 x+2 y \geq 4000$
Similarly for model C,
$30 x+40 y \geq 4800 \Rightarrow 3 x+4 y \geq 480$
and $x \geq 0, y \geq 0$
It costs ₹ 12,000 and $₹ 15000$ to operate the factories I and II each day.
$\therefore$ Required LPP is
Minimise $Z=12000 x+15000 y$ subject to the constraints

$$
\begin{align*}
5 x+4 y & \geq 640  \tag{i}\\
5 x+2 y & \geq 400  \tag{ii}\\
3 x+4 y & \geq 480  \tag{iii}\\
x & \geq 0, y \geq 0 \tag{iv}
\end{align*}
$$

Table for (i) equation $5 x+4 y=640$

| $x$ | 0 | 128 |
| :---: | :---: | :---: |
| $y$ | 160 | 0 |

Table for (ii) equation $5 x+2 y=400$

| $x$ | 0 | 80 |
| :---: | :---: | :---: |
| $y$ | 200 | 0 |

Table for (iii) equation $3 x+4 y=480$

| $x$ | 0 | 160 |
| :---: | :---: | :---: |
| $y$ | 120 | 0 |



On solving eq. (i) and (iii), we get $x=80, y=60$

On solving eq. (i) and (ii) we get
$x=32$ and $y=120$
From the graph, we see that the feasible region $A B C D$ is open unbounded whose corners are $\mathrm{A}(160,0), \mathrm{B}(80,60), \mathrm{C}(32,120)$ and $\mathrm{D}(0,200)$.
Let us find the values of Z .

| Corner points | Value of $\mathrm{Z}=12000 x+15000 y$ |
| :---: | :---: |
| $\mathrm{~A}(160,0)$ | $\mathrm{Z}=12000(160)+0=1920000$ |
| $\mathrm{~B}(80,60)$ | $\mathrm{Z}=12000(80)+15000(60)$ <br> $=1860000$ |
| $\mathrm{C}(32,120)$ | $\mathrm{Z}=12000(32)+15000(120)$ <br> $=2184000$ |
| $\mathrm{D}(0,200)$ | $\mathrm{Z}=0+15000(200)=3000000$ |

From the above table, it is clear that the value of $Z=1860000$ may or may not be minimum for an open unbounded region. Now, to decide this, we draw a graph of

$$
\begin{aligned}
& & 12000 x+15000 y & <1860000 \\
\Rightarrow & & 4 x+5 y & <620
\end{aligned}
$$

and we have to check whether there is a common point in this feasible region or not.
So, from the graph, there is no common point.
$\therefore Z=12000 x+15000 y$ has minimum value 1860000 at $(80,60)$.
Factory I : 80 days
Factory II: 60 days.
Q25. Maximise and minimise $Z=3 x-4 y$ subject to $x-2 y \leq 0$, $-3 x+y \leq 4, x-y \leq 6$ and $x, y \geq 0$.
Sol. Given LPP is
Maximise and minimise $Z=3 x-4 y$ subject to

| $x-2 y \leq 0$ | ...(i) | $x$ | 0 | 2 |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $y$ | 0 | 1 |
| $-3 x+y \leq 4$ | ...(ii) | $x$ | 0 | -4/3 |
|  |  | $y$ | 4 | 0 |
| $x-y \leq 6$ | ...(iii) | $x$ | 0 | 6 |
|  |  | $y$ | -6 | 0 |
| $x, y \geq 0$ | ...(iv) |  |  |  |

and $\quad x, y \geq 0$

From the graph, we see that AOB is open unbounded region whose corners are $\mathrm{O}(0,0), \mathrm{A}(0,4), \mathrm{B}(12,6)$.
Let us evaluate the value of Z


| Corner points | Value of $\mathrm{Z}=3 x-4 y$ |
| :---: | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=0$ |
| $\mathrm{~A}(0,4)$ | $\mathrm{Z}=0-4(4)=-16$ |
| $\mathrm{~B}(12,6)$ | $\mathrm{Z}=3(12)-4(6)=12$ |
| $\leftarrow$ | $\leftarrow$ Minimum |
| $\leftarrow$ Maximum |  |

For this unbounded region, the value of Z may or may not be -16 . So to decide it, we draw a graph of inequality $3 x-4 y<-16$ and check whether the open half plane has common points with feasible region or not. But from the graph, we see that it has common points with the feasible region, so it will have not minimum value of $Z$. Similarly for maximum value, we draw the graph of inequality $3 x-4 y>12$ in which there is no common point with the feasible region.
Hence, the maximum value of Z is 12 .

## OBJECTIVE TYPE QUESTIONS

Choose the correct answer from the given four options in each of the Exercises 26 to 34 .

Q26. The corner points of the feasible region determined by the system of linear constraints are $(0,0),(0,40),(20,40),(60,20)$, $(60,0)$. The objective function is $Z=4 x+3 y$. Compare the quantity in Column A and Column B

| Column A | Column B |
| :---: | :---: |
| Maximum of Z | 325 |

(a) The quantity in column A is greater.
(b) The quantity in column $B$ is greater
(c) The two quantities are equal
(d) The relationship cannot be determined on the basis of the information supplied.

Sol.

| Corner points | Value of $\mathrm{Z}=4 x+3 y$ |
| :---: | :--- |
|  | $\mathrm{Z}=0$ |
|  | $\mathrm{Z}=0+3(40)=120$ |
|  | $\mathrm{Z}=4(20)+3(40)=200$ |
|  |  |
| $(60,20)$ | $\mathrm{Z}=4(60)+3(20)=300$ |
| $\rightarrow$ Maximum |  |
|  | $\mathrm{Z}=4(60)+3(0)=240$ |
|  |  |

Hence, the correct option is $(b)$.
Q27. The feasible solution for a LPP is shown in figure. Let $Z=3 x-4 y$ be the objective function. Minimum of Z occurs at
(a) $(0,0)$
(b) $(0,8)$
(c) $(5,0)$
(d) $(4,10)$


Sol.

| Corner points | Value of $\mathrm{Z}=3 x-4 y$ |
| :---: | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{Z}=0$ |
| $\mathrm{~A}(5,0)$ | $\mathrm{Z}=3(5)-0=15$ |
| $\mathrm{~B}(6,5)$ | $\mathrm{Z}=3(6)-4(5)=-2$ |
| $\mathrm{C}(6,8)$ | $\mathrm{Z}=3(6)-4(8)=-14$ |
| $\mathrm{D}(4,10)$ | $\mathrm{Z}=3(4)-4(10)=-28$ |
| $\mathrm{E}(0,8)$ | $\mathrm{Z}=3(0)-4(8)=-32$ |$\leftarrow$ Minimum

Hence, the correct option is (b).

Q28. Refer to Exercise 27. Maximum of Z occurs at
(a) $(5,0)$
(b) $(6,5)$
(c) $(6,8)$
(d) $(4,10)$

Sol. According to solution of Q. 27, the maximum value of Z is 15 at $\mathrm{A}(5,0)$.
Hence, the correct option is (a).
Q29. Refer to Exercise 27. (Maximum value of $\mathrm{Z}+$ Minimum value of $Z$ ) is equal to
(a) 13
(b) 1
(c) -13
(d) -17

Sol. According to the solution of Q. 27, Maximum value of $\mathrm{Z}=15$ and Minimum value of $Z=-32$
So, the sum of Maximum value and Minimum value of $Z$

$$
=15+(-32)=-17
$$

Hence, the correct option is (d).
Q30. The feasible region for an LPP is shown in the figure. Let $\mathrm{F}=3 x-4 y$ be the objective function. Maximum value of F is
(a) 0
(b) 8
(c) 12
(d) -18


Sol. The feasible region is shown in the figure for which the objective function $\mathrm{F}=3 x-4 y$

| Corner point | Value of $F=3 x-4 y$ |
| :---: | :--- |
| $\mathrm{O}(0,0)$ | $\mathrm{F}=0$ |
| $\mathrm{~A}(12,6)$ | $\mathrm{F}=3(12)-4(6)=12$ |
| $\mathrm{~B}(0,4)$ | $\mathrm{F}=0-4(4)=-16$ |
| $\leftarrow$ | $\leftarrow$ Maximum |
| $\leftarrow$ Minimum |  |

Hence, the correct option is (c).
Q31. Refer to Exercise 30. Minimum value of F is
(a) 0
(b) -16
(c) 12
(d) does not exist

Sol. According to the solution of Q. 30, the minimum value of F is -16 at $(0,4)$.
Hence, the correct option is (b).

Q32. Corner points of the feasible region for an LPP are (0, 2), (3, 0), $(6,0),(6,8)$ and $(0,5)$.
Let $\mathrm{F}=4 x+6 y$ be the objective function.
The minimum value of $F$ occurs at
(a) $(0,2)$ only
(b) $(3,0)$ only
(c) the mid-point of the line segment joining the points $(0,2)$ and $(3,0)$ only
(d) any point on the line segment joining the points $(0,2)$ and $(3,0)$

Sol.

| Corner points | Value of $F=4 x+6 y$ |
| :---: | :--- |
| $(0,2)$ | $\mathrm{Z}=4(0)+6(2)=12$ |
| $(3,0)$ | $\mathrm{Z}=4(3)+6(0)=12$ |
| $(6,0)$ | $\mathrm{Z}=4(6)+6(0)=24$ |
| $(6,8)$ | $\mathrm{Z}=4(6)+6(8)=72$ |
| $(0,5)$ | $\mathrm{Z}=4(0)+6(5)=30$ |

The minimum value of F occurs at any point on the line segment joining the points $(0,2)$ and $(3,0)$.
Hence, the correct option is $(d)$.
Q33. Refer to Exercise 32, Maximum of $\mathrm{F}-$ Minimum of $\mathrm{F}=$
(a) 60
(b) 48
(c) 42
(d) 18

Sol. According to the solution of Q. 32,
Maximum value of $\mathrm{F}-$ Minimum value of $\mathrm{F}=72-12=60$
Hence, the correct option is (a).
Q34. Corner points of the feasible region determined by the system of linear constraints are $(0,3),(1,1)$ and $(3,0)$.
Let $\mathrm{Z}=p x+q y$, where $p, q>0$. Condition on $p$ and $q$ so that the minimum of $Z$ occurs at $(3,0)$ and $(1,1)$ is
(a) $p=2 q$
(b) $p=\frac{q}{2}$
(c) $p=3 q$
(d) $p=q$

Sol.

| Corner points | Value of $\mathrm{Z}=p x+q y ; p, q>0$ |
| :--- | :--- |
| $(0,3)$ | $\mathrm{Z}=p(0)+q(3)=3 q$ |
| $(1,1)$ | $\mathrm{Z}=p(1)+q(1)=p+q$ |
| $(3,0)$ | $\mathrm{Z}=p(3)+q(0)=3 p$ |

So, condition of $p$ and $q$ so that the minimum of $Z$ occurs at $(3,0)$ and $(1,1)$ is
$p+q=3 p \Rightarrow p-3 p+q=0 \Rightarrow p=\frac{q}{2}$.
Hence, the correct option is (b).

Fill in the blanks in each of the Exercises 35 to 41.
Q35. In a LPP, the linear inequalities or restrictions on the variables are called
Sol. constraints.
Q36. In a LPP, the objective function is always $\qquad$ ..

Sol. linear.
Q37. If the feasible region for a LPP is $\qquad$ then the optimal value of the objective function $\mathrm{Z}=a x+b y$ may or may not exist.
Sol. open unbounded
Q38. In a LPP, if the objective function $\mathrm{Z}=a x+b y$ has the same maximum value at two corner points of the feasible region, then every point on the line segment joining these two points give the same $\qquad$ value.
Sol. maximum
Q39. A feasible region of a system of linear inequalities is said to be ................. if it can be enclosed within a circle.
Sol. bounded
Q40. A corner point of a feasible region is a point in the region which is the $\qquad$ of two boundary lines.
Sol. intersection
Q41. The feasible region for an LPP is always a. polygon. Sol. convex
State whether the statements in Exercises 42 to 45 are True or False.
Q42. If the feasible region for a LPP is unbounded, maximum or minimum of the objective function $\mathrm{Z}=a x+b y$ may or may not exist.
Sol. True.
Q43. Maximum value of the objective function
$\mathrm{Z}=a x+b y$ in a LPP always occurs at only one corner point of the feasible region.
Sol. False.
Q44. In a LPP, the minimum value of the objective function $\mathrm{Z}=a x+b y$ is always 0 if the origin is one of the corner point of the feasible region.
Sol. False.
Q45. In a LPP, the maximum value of the objective function $\mathrm{Z}=a x+b y$ is always finite.
Sol. True.

