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## Exercise 15.1

1. In a cricket match, a batswoman hits a boundary 6 times out of 30 balls she plays. Find the probability that she did not hit a boundary.

Solution:

According to the question,

Total number of balls = 30

Numbers of boundary = 6

Number of time batswoman didn't hit boundary = 30 - 6 = 24

Probability she did not hit a boundary = 24/30 = 4/5

2. 1500 families with 2 children were selected randomly, and the following data were recorded:

Number of girls in a family	2	1	0
Number of families	475	814	211

Compute the probability of a family, chosen at random, having

(ii) 1 girl

(iii) No girl

Also check whether the sum of these probabilities is 1.

Solution:

Total numbers of families = 1500

Numbers of families having 2 girls = 475(i)

Probability = Numbers of families having 2 girls/Total numbers of families

(ii) Numbers of families having 1 girl = 814

Probability = Numbers of families having 1 girl /Total numbers of families

= 814/1500 = 407/750

(iii) Numbers of families having 0 girls = 211

> Probability = Numbers of families having 0 girls/Total numbers of families =211/1500

Sum of the probability = 
$$(19/60)+(407/750)+(211/1500)$$
  
=  $(475+814+211)/1500$ 

Yes, the sum of these probabilities is 1.

3. Refer to Example 5, Section 14.4, Chapter 14. Find the probability that a student of the class was born in August.

Solution:



Fig. 14.1

Total numbers of students in the class = 40

Numbers of students born in August = 6

The probability that a student of the class was born in August, = 6/40 = 3/20

4. Three coins are tossed simultaneously 200 times with the following frequencies of different outcomes:

Outcome	3 heads	2 heads	1 head	No head	
Frequency	23	72	77	28	

If the three coins are simultaneously tossed again, compute the probability of 2 heads coming up.

### Solution:

Number of times 2 heads come up = 72 Total number of times the coins were tossed = 200

 $\therefore$ , the probability of 2 heads coming up = 72/200 = 9/25

5. An organisation selected 2400 families at random and surveyed them to determine a relationship between income level and the number of vehicles in a family. The information gathered is listed in the table below:

Monthly income	Vehicles per family					
(in ₹)	0	1	2	Above 2		
Less than 7000	10	160	25	0		
7000-10000	0	305	27	2		
10000-13000	1	535	29	1		
13000-16000	2	469	59	25		
16000 or more	1	579	82	88		

Suppose a family is chosen. Find the probability that the family chosen is

- (i) earning ₹10000 13000 per month and owning exactly 2 vehicles.
- (ii) earning ₹16000 or more per month and owning exactly 1 vehicle.
- (iii) earning less than ₹7000 per month and does not own any vehicle.
- (iv) earning ₹13000 16000 per month and owning more than 2 vehicles.
- (v) owning not more than 1 vehicle.

## Solution:

Total number of families = 2400

- (i) Numbers of families earning ₹10000 −13000 per month and owning exactly 2 vehicles = 29 ∴, the probability that the family chosen is earning ₹10000 − 13000 per month and owning exactly 2 vehicles = 29/2400
- (ii) Number of families earning ₹16000 or more per month and owning exactly 1 vehicle = 579 ∴, the probability that the family chosen is earning ₹16000 or more per month and owning exactly 1 vehicle = 579/2400
- (iii) Number of families earning less than ₹7000 per month and does not own any vehicle = 10 ∴, the probability that the family chosen is earning less than ₹7000 per month and does not own any vehicle = 10/2400 = 1/240
- (iv) Number of families earning ₹13000-16000 per month and owning more than 2 vehicles = 25 ∴, the probability that the family chosen is earning ₹13000 – 16000 per month and owning more than 2 vehicles = 25/2400 = 1/96
- (v) Number of families owning not more than 1 vehicle = 10+160+0+305+1+535+2+469+1+579= 2062
  - $\therefore$ , the probability that the family chosen owns not more than 1 vehicle = 2062/2400 = 1031/1200
- 6. Refer to Table 14.7, Chapter 14.
  - (i) Find the probability that a student obtained less than 20% in the mathematics test.
  - (ii) Find the probability that a student obtained marks 60 or above.

Solution:

Marks	Number of students
0 - 20	7
20 - 30	10
30 - 40	10
40 - 50	20
50 - 60	20
60 - 70	15
70 - above	8
Total	90

Total number of students = 90

- (i) Number of students who obtained less than 20% in the mathematics test = 7
  ∴, the probability that a student obtained less than 20% in the mathematics test = 7/90
- (ii) Number of students who obtained marks 60 or above = 15+8=23  $\therefore$ , the probability that a student obtained marks 60 or above = 23/90
- 7. To know the opinion of the students about the subject statistics, a survey of 200 students was conducted. The data is recorded in the following table.

Opinion	Number of students				
like	135				
dislike	65				

## Find the probability that a student chosen at random

(i) likes statistics, (ii) does not like it.

#### Solution:

Total number of students = 135+65 = 200

- (i) Number of students who like statistics = 135
  ∴, the probability that a student likes statistics = 135/200 = 27/40
- (ii) Number of students who do not like statistics = 65 ∴, the probability that a student does not like statistics = 65/200 = 13/40
- 8. Refer to Q.2, Exercise 14.2. What is the empirical probability that an engineer lives:
  - (i) less than 7 km from her place of work?
  - (ii) more than or equal to 7 km from her place of work?
  - (iii) Within 1/2 km from her place of work?

### Solution:

The distance (in km) of 40 engineers from their residence to their place of work were found as follows:

Total numbers of engineers = 40

- (i) Number of engineers living less than 7 km from their place of work = 9
  - :, the probability that an engineer lives less than 7 km from her place of work = 9/40
- (ii) Number of engineers living more than or equal to 7 km from their place of work = 40-9 = 31
  - $\therefore$ , probability that an engineer lives more than or equal to 7 km from her place of work = 31/40
- (iii) Number of engineers living within  $\frac{1}{2}$  km from their place of work = 0
  - $\therefore$ , the probability that an engineer lives within  $\frac{1}{2}$  km from her place of work = 0/40 = 0
- Activity: Note the frequency of two-wheelers, three-wheelers and four-wheelers going past during a time interval, in front of your school gate. Find the probability that any one vehicle out of the total vehicles you have observed is a two-wheeler.

### Solution:

The question is an activity to be performed by the students.

Hence, perform the activity by yourself and note down your inference.

10. Activity: Ask all the students in your class to write a 3-digit number. Choose any student from the room at random. What is the probability that the number written by her/him is divisible by 3? Remember that a number is divisible by 3, if the sum of its digits is divisible by 3.

## Solution:

The question is an activity to be performed by the students.

Hence, perform the activity by yourself and note down your inference.

11. Eleven bags of wheat flour, each marked 5 kg, actually contained the following weights of flour (in kg):

4.97 5.05 5.08 5.03 5.00 5.06 5.08 4.98 5.04 5.07 5.00

Find the probability that any of these bags chosen at random contains more than 5 kg of flour.

## Solution:

Total number of bags present = 11

Number of bags containing more than 5 kg of flour = 7

 $\therefore$ , the probability that any of the bags chosen at random contains more than 5 kg of flour = 7/11

12. In Q.5, Exercise 14.2, you were asked to prepare a frequency distribution table, regarding the concentration of sulphur dioxide in the air in parts per million of a certain city for 30 days. Using this table, find the probability of the concentration of sulphur dioxide in the interval 0.12-0.16 on any of these days.

The data obtained for 30 days is as follows:

0.03	0.08	0.08	0.09	0.04	0.17	0.16	0.05	0.02	0.06	0.18	0.20
0.11	0.08	0.12	0.13	0.22	0.07	0.08	0.01	0.10	0.06	0.09	0.18
0.11	0.07	0.05	0.07	0.01	0.04						

#### Solution:

Total number of days in which the data was recorded = 30 days

Numbers of days in which sulphur dioxide was present in between the interval 0.12-0.16=2

 $\therefore$ , the probability of the concentration of sulphur dioxide in the interval 0.12-0.16 on any of these days = 2/30 = 1/15

13. In Q.1, Exercise 14.2, you were asked to prepare a frequency distribution table regarding the blood groups of 30 students of a class. Use this table to determine the probability that a student of this class, selected at random, has blood group AB.

The blood groups of 30 students of Class VIII are recorded as follows:

A, B, O, O, AB, O, A, O, B, A, O, B, A, O, O, A, AB, O, A, A, O, O, AB, B, A, O, B, A, B, O.

### Solution:

Total numbers of students = 30

Number of students having blood group AB = 3

 $\therefore$ , the probability that a student of this class, selected at random, has blood group AB = 3/30 = 1/10