An isosceles right triangle has area 8 cm<sup>2</sup>. The length of its hypotenuse is:



(a)  $10\sqrt{3}$  m<sup>2</sup> (b)  $15\sqrt{3}$  m<sup>2</sup> (c)  $20\sqrt{3}$  m<sup>2</sup> (d)  $100\sqrt{3}$  m<sup>2</sup>

**Sol.** Perimeter of triangle = 3a

Now,

$$3a = 60 \Rightarrow a = 60 \div 3 =$$

Area of equilateral 
$$\Delta = \frac{\sqrt{3}}{4}$$
 (side)<sup>2</sup> =  $\frac{\sqrt{3}}{4} \times (20)^2 = 100\sqrt{3}$  m<sup>2</sup>

20 m

Hence, (d) is the correct answer.

**3.** The sides of a triangle are 56 cm, 60 cm and 52 cm long. Then the area of the triangle is

(a)  $1322 \text{ cm}^2$  (b)  $1311 \text{ cm}^2$  (c)  $1344 \text{ cm}^2$  (d)  $1392 \text{ cm}^2$ 

Sol. Since, the three sides of triangle are a = 56 cm, b = 60 cm and c = 52 cm. Then, the semi-perimeter of triangle,

$$s = \frac{a+b+c}{2} = \frac{56+60+52}{2} = \frac{168}{2} = 84 \text{ cm}$$
  
Area of a triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$  [By Heron's formula]

$$= \sqrt{84(84 - 56)(84 - 60)(84 - 52)}$$
  
=  $\sqrt{84 \times 28 \times 24 \times 32}$   
=  $\sqrt{4 \times 7 \times 3 \times 4 \times 7 \times 4 \times 2 \times 3 \times 4 \times 4 \times 2}$   
=  $\sqrt{(4)^6 \times (7)^2 \times (3)^2}$   
=  $(4)^3 \times 7 \times 3$   
=  $1344 \text{ cm}^2$ 

Hence, the area of triangle is  $1344 \text{ cm}^2$ . Therefore, (*c*) is the correct answer.

4. The area of an equilateral triangle with side  $2\sqrt{3}$  cm is (a) 5.196 cm<sup>2</sup>(b) 0.866 cm<sup>2</sup>(c) 3.496 cm<sup>2</sup>(d) 1.732 cm<sup>2</sup>

Sol. Area of equilateral 
$$\Delta = \frac{\sqrt{3}}{4} (\text{side})^2$$
  
=  $\frac{\sqrt{3}}{4} (2\sqrt{3})^2 = 3\sqrt{3} = 3 \times 1.732$   
= 5.196 cm<sup>2</sup>

Hence, (a) is the correct answer.

5. The length of each side of an equilateral triangle having an area  $9\sqrt{3}$  cm<sup>2</sup> is

(a) 8 cm (b) 36 cm (c) 4 cm (d) 6 cm

**Sol.** Area of equilateral  $\Delta i.e.$ ,  $9\sqrt{3} = \frac{\sqrt{3}}{4}$  (Side)<sup>2</sup>

 $(\text{Side})^2 = \frac{9\sqrt{3} \times 4}{\sqrt{3}} = 36$ 

 $\Rightarrow$ 

 $\Rightarrow$ 

 $\therefore \qquad \text{Side} = \pm \sqrt{36} = 6 \text{ cm}$ Hence, (d) is the correct answer.

6. If the area of equilateral triangle is  $16\sqrt{3}$  cm<sup>2</sup>, then the perimeter of the triangle is

(a) 48 cm (b) 24 cm (c) 12 cm (d) 36 cm

**Sol.** Area of equilateral  $\Delta = \frac{\sqrt{3}}{4}$  (Side)<sup>2</sup>

$$16\sqrt{3} = \frac{\sqrt{3}}{4}$$
 (Side)<sup>2</sup>

$$\Rightarrow$$

$$(\text{Side})^2 = \frac{16\sqrt{3} \times 4}{\sqrt{3}} = 64$$
$$\text{Side} = \pm\sqrt{64} = 8 \text{ cm}$$

\_

:. Side =  $+\sqrt{64} = 8$  cm So, perimeter of triangle = 8 + 8 + 8 = 24 cm Hence, (*b*) is the correct answer

**7.** The sides of a triangle are 35 cm, 54 cm and 61 cm, respectively. The length of its longest altitude is

(a) $16\sqrt{5}$ cm	<i>(b)</i>	10√5	cm
---------------------	------------	------	----

(c) $24\sqrt{5}$ cm	( <i>d</i> ) 28 cm
---------------------	--------------------

Sol. Sides of the triangle are 35 cm, 54 cm and 61 cm

$$s = \frac{35 + 54 + 61}{2} = 75 \text{ cm}$$
Area of  $\Delta = \sqrt{75(75 - 35)(75 - 54)(75 - 61)}$ 

$$= \sqrt{75 \times 40 \times 21 \times 14}$$

$$= \sqrt{5 \times 5 \times 3 \times 2 \times 2 \times 2 \times 5 \times 3 \times 7 \times 7 \times 2}$$

$$= 5 \times 3 \times 2 \times 2 \times 7 \sqrt{5} = 420\sqrt{5} \text{ cm}^2$$

Now, longest altitude will be the perpendicular on the smallest side of the triangle from the opposite vertex.

$$\therefore \text{ Length of longest altitude} = \frac{2(\text{Area of } \Delta)}{35}$$
$$= \frac{2 \times 420\sqrt{5}}{35} = 24\sqrt{5} \text{ cm}$$

Hence, (c) is the correct answer.

**8.** The area of an isosceles triangle having base 2 cm and length of its equal sides 4 cm is

(a) $\sqrt{15}$ cm <sup>2</sup>	(b) $\sqrt{\frac{15}{2}}$ cm <sup>2</sup>
(c) $2\sqrt{15}$ cm <sup>2</sup>	( <i>d</i> ) $4\sqrt{15}$ cm <sup>2</sup>

 $s = \frac{4+4+2}{2} = 5 \text{ cm}$ 

Sol. Here,

Area of 
$$\Delta = \sqrt{5(5-2)(5-4)(5-4)}$$
  
=  $\sqrt{5 \times 3 \times 1 \times 1} = \sqrt{15}$  cm<sup>2</sup>

Hence, (*a*) is the correct answer.

**9.** The edge of a triangular board are 6 cm, 8 cm and 10 cm. The cost of painting it at the rate of 9 paise per cm<sup>2</sup> is

(a) ₹2.00 (b) ₹2.16 (c) ₹2.48 (d) ₹3.00 Sol. Here,  $2s = 6 + 8 + 10 = 24 \Rightarrow s = 24 \div 2 = 12$  cm

Area of 
$$\Delta = \sqrt{12(12-6)(12-8)(12-10)}$$
  
=  $\sqrt{2 \times 6 \times 6 \times 4 \times 2} = 2 \times 6 \times 2 = 24 \text{ cm}^2$ 

Cost of painting at the rate of 9 paise per cm<sup>2</sup> =  $\mathbf{\xi}$  (24 × 0.09) =  $\mathbf{\xi}$  2.16 Hence, (*b*) is the correct answer.

Write whether the following statements are True or False. Justify your answer.

1. The area of a triangle with base 4 cm and height 6 cm is  $24 \text{ cm}^2$ .

- Area of  $\Delta = \frac{1}{2} \times \text{base} \times \text{height} = \frac{1}{2} \times 4 \times 6 = 12 \text{cm}^2$ Sol. Hence, the given statement is false.
  - 2. The area of  $\triangle$  ABC is 8 cm<sup>2</sup> in which AB = AC = 4 cm and  $\angle$ A = 90°.

Sol. Area of 
$$\Delta = \frac{1}{2} \times \text{base} \times \text{height}$$
  
 $= \frac{1}{2} \times 4 \times 4 = 8 \text{ cm}^2$   
Hence, the given statement is true.

Hence, the given statement is true.

- 3. The area of the isosceles triangle is  $\frac{5}{4}\sqrt{11}$  cm<sup>2</sup> if the perimeter 11 is and the base is 5 cm.
- Sol. Let the equal sides of the isosceles triangle be 'a' and base of the triangle be '*b*'.

Perimeter of 
$$\Delta = 5 + a + a = 11$$
  
 $\Rightarrow \qquad 2a = 11 - 5 = 6; a = 6 \div 2 = 3 \text{ cm}$   
Area of isosceles  $\Delta = \frac{b}{4}\sqrt{4a^2 - b^2} = \frac{5}{4}\sqrt{4(3)^2 - 5^2}$   
 $= \frac{5}{4}\sqrt{11} \text{ cm}^2$ 

Hence the given statement is true.

4. The area of the equilateral triangle is  $20\sqrt{3}$  cm<sup>2</sup> whose each side is 8 cm.

**Sol.** Area of equilateral 
$$\Delta = \frac{\sqrt{3}}{4} (\text{side})^2$$

$$=\frac{\sqrt{3}}{4}(8)^2 = \frac{\sqrt{3}}{4} \times 64 = 16\sqrt{3} \text{ cm}^2$$

Hence, the given statement is false.

- 5. If the side of a rhombus is 10 cm and one diagonal is 16 cm, the area of the rhombus 96 cm<sup>2</sup>.
- **Sol.** Let ABCD be the rhombus whose one diagonal AC is 16 cm. Each side of rhombus is 10 cm.

We know that diagonal of a rhombus bisect each other at right angles, so

OA = OC = 8 cm and OB = OD.In ΔAOB, we have ∠AOB = 90°  $\therefore AB^2 = OA^2 + OB^2$  $\Rightarrow OB^2 = AB^2 - OA^2$  $= (10)^2 - 8^2 = 100 - 64 = 36$  $\therefore OB = +\sqrt{36} = 6 \text{ cm}$  $\therefore DB = 2(OB) = 2 \times 6 = 12 \text{ cm}$ 

Hence, area of rhombus =  $\frac{1}{2} \times \text{Product of diagonals}$ =  $\frac{1}{2} \times 16 \times 12 = 96 \text{ cm}^2$ 

Hence, the given statement is true.

- **6.** The base and the corresponding altitude of a parallelogram are 10 cm and 3.5 cm respectively. The area of the parallelogram is 30 cm<sup>2</sup>.
- **Sol.** The base of the parallelogram is 10 cm and the corresponding altitude is 3.5 cm.

Area of  $||gm| = base \times corresponding altitude$ = 10 cm × 3.5 cm = 35 cm<sup>2</sup>.

Hence, the given statement is false.

- 7. The area of a regular hexagon of side 'a' is the sum of the areas of the five equilateral triangles with side *a*.
- **Sol.** We see a regular hexagon is divided into six equilateral triangles. So, the area of a regular hexagon of side '*a*' is the sum of the areas of the six equilateral triangles with side *a*.



Hence, the given statement that the area of a regular hexagon of side '*a*' is the sum of the areas of the five equilateral triangles with side *a* is false.

8. The cost of levelling the ground in the form of a triangle having the sides 51 m, 37 m and 20 m at the rate of ₹ 3 per m<sup>2</sup> is ₹ 918.

Sol. We have  

$$2s = 51 \text{ m} + 37 \text{ m} + 20 \text{ m} = 108 \text{ m}$$

$$s = 108 \div 2 = 54 \text{ m}$$
Area of  $\Delta = \sqrt{s(s-a)(s-b)(s-c)}$ 

$$= \sqrt{54(54-51)(54-37)(54-20)}$$
  
=  $\sqrt{54\times3\times17\times34}$   
=  $\sqrt{3\times3\times3\times2\times3\times17\times17\times2}$   
=  $3\times3\times17\times2$  = 306 m<sup>2</sup>

Cost of levelling the ground =  $\gtrless$  (306 × 3) =  $\gtrless$  918 Hence, the given statement is true.

- **9.** In a triangle, the sides are given as 11 cm, 12 cm and 13 cm. The length of the altitude is 10.25 cm corresponding to the side having length 12 cm.
- **Sol.** We have the length of the altitude corresponding to the side having length 12 cm.

$$2s = 11 \text{ cm} + 12 \text{ cm} + 13 \text{ cm} = 36 \text{ cm}$$

$$s = 36 \div 2 = 18 \text{ cm}$$
Area of  $\Delta = \sqrt{s(s-a)(s-b)(s-c)}$ 

$$= \sqrt{18(18-11)(18-12)(18-13)}$$

$$= \sqrt{18 \times 7 \times 6 \times 5} = \sqrt{2 \times 3 \times 3 \times 7 \times 2 \times 3 \times 5}$$

$$= 2 \times 3\sqrt{105} = 6\sqrt{105} \text{ cm}^2$$
Length of altitude  $= \frac{2 \text{ Area of } \Delta}{\text{Base}} = \frac{2 \times 6\sqrt{105}}{12}$ 

$$= \sqrt{105} = 10.25 \text{ cm}$$
Hence, the given statement is true

Hence, the given statement is true.

1. Find the cost of laying grass in a triangular field of sides 50 m, 65 m and 65 m at the rate of ₹ 7 per m<sup>2</sup>.

Sol. We have, 2s = 50 m + 65 m + 65 m = 180 m  $\Rightarrow \qquad s = 180 \div 2 = 90 \text{ m}$ Area of  $\Delta = \sqrt{s(s-a)(s-b)(s-c)}$  $= \sqrt{90(90-50)(90-65)(90-65)}$ 

$$= \sqrt{90 \times 40 \times 25 \times 25} = 60 \times 25$$
$$= 1500 \,\mathrm{m}^2$$

Cost of laying grass at the rate of  $\overline{\mathbf{e}}7$  per m<sup>2</sup> =  $\overline{\mathbf{e}}(1500 \times 7) = \overline{\mathbf{e}}10,500$ 

- 2. The triangular side walls of a flyover have been used for advertisements. The sides of the walls are 13 m, 14 m, and 15 m. The advertisement yield an earning of ₹ 2000 per m<sup>2</sup> a year. A company hired one of its walls for 6 months. How much rent did it pay?
- **Sol.** The sides of triangular side walls of a flyover which have been used for advertisements are 13 m, 14 m, 15 m.

$$s = \frac{13 + 14 + 15}{2} = \frac{42}{2} = 21 \text{ m}$$
  
=  $\sqrt{21(21 - 13)(21 - 14)(21 - 15)}$   
=  $\sqrt{21 \times 8 \times 7 \times 6}$   
=  $\sqrt{7 \times 3 \times 2 \times 2 \times 2 \times 7 \times 3 \times 2}$   
=  $7 \times 3 \times 2 \times 2 = 84 \text{ m}^2$ 

It is given that the advertisement yield an earning of  $\mathbf{E}$  2,000 per m<sup>2</sup> a year.

 $\therefore \quad \text{Rent for 1 } \text{m}^2 \text{ for 1 } \text{year} = ₹ 2000$ 

So, rent for 1 m<sup>2</sup> for 6 months or  $\frac{1}{2}$  year =  $\overline{\langle} (\frac{1}{2} \times 2000) = \overline{\langle} 1,000$ .

- $\therefore \text{ Rent for } 84 \text{ m}^2 \text{ for } 6 \text{ months} = \texttt{P}(1000 \times 84) = \texttt{P} \texttt{84,000}.$
- **3.** From a point in the interior of an equilateral triangle, perpendiculars are drawn on the three sides. The lengths of the perpendiculars are 14 cm, 10 cm and 6 cm. Find the area of the triangle.
- **Sol.** Let ABC be an equilateral triangle, O be the interior point and OQ, OR and OC are the perpendiculars drawn from point O. Let the sides of an equilateral triangle be *a* m.

Area of  $\triangle OAB = \frac{1}{2} \times AB \times OP$ 

А

[:: Area of a triangle = 
$$\frac{1}{2} \times (base \times height)$$
]

$$= \frac{1}{2} \times a \times 14 = 7a \operatorname{cm}^2 \qquad \dots (1)$$

Area of 
$$\triangle OBC = \frac{1}{2} \times BC \times OQ = \frac{1}{2} \times a \times 10$$
  
= 5a cm<sup>2</sup> ... (2)

... (4)

...

 $\Rightarrow$ 

 $\Rightarrow$ 

Area of 
$$\triangle OAC$$
 =  $\frac{1}{2} \times AC \times OR = \frac{1}{2} \times a \times 6$   
=  $3a \text{ cm}^2$  ...(3)  
Area of an equilateral  $\triangle ABC$   
= Area of  $(\triangle OAB + \triangle OBC + \triangle OAC)$   
=  $(7a + 5a + 3a) \text{ cm}^2$   
=  $15a \text{ cm}^2$  ...(4)

We have, semi-perimeter 
$$s = \frac{a+a+a}{2}$$

$$\Rightarrow \qquad s = \frac{3a}{2} \mathrm{cm}$$

:. Area of an equilateral  $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$ [By Heron's formula] 3a(3a)(3a)(3a)

$$= \sqrt{\frac{3a}{2}} \left(\frac{3a}{2} - a\right) \left(\frac{3a}{2} - a\right) \left(\frac{3a}{2} - a\right)$$
$$= \sqrt{\frac{3a}{2}} \times \frac{a}{2} \times \frac{a}{2} \times \frac{a}{2}$$
$$= \frac{\sqrt{3}}{4} a^{2} \qquad \dots (5)$$

From equations (4) and (5), we get

$$\frac{\sqrt{3}}{4}a^2 = 15a$$
$$a = \frac{15 \times 4}{\sqrt{3}} = \frac{60}{\sqrt{3}}$$
$$a = \frac{60}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 20\sqrt{3} \text{ cm}$$

On putting  $a = 20\sqrt{3}$  in equation (5), we get

Area of 
$$\triangle ABC = \frac{\sqrt{3}}{4} (20\sqrt{3})^2 = \frac{\sqrt{3}}{4} \times 400 \times 3 = 300\sqrt{3} \text{ cm}^2$$

Hence, the area of an equilateral triangle is  $300\sqrt{3}$  cm<sup>2</sup>

- 4. The perimeter of an isosceles triangle is 32 cm. The ratio of the equal side to its base is 3 : 2. Find the area of the triangle.
- Sol. As the sides of the equal side to the base of an isosceles triangle is 3 : 2, so let the sides of an isosceles triangle be 3x, 3x and 2x. Now, perimeter of triangle = 3x + 3x + 2x = 8xGiven perimeter of the triangle = 32 m $\therefore 8x = 32; x = 32 \div 8 = 4$

So, the sides of the isosceles triangle are  $(3 \times 4)$  cm,  $(3 \times 4)$  cm,  $(2 \times 4)$  cm *i.e.*, 12 cm, 12 cm and 8 cm

$$\therefore \qquad s = \frac{12 + 12 + 8}{2} = \frac{32}{2} = 16 \text{ cm}$$
$$= \sqrt{16(16 - 12)(16 - 12)(16 - 8)}$$
$$= \sqrt{16 \times 4 \times 4 \times 8} = \sqrt{4 \times 4 \times 4 \times 4 \times 4 \times 2}$$
$$= 4 \times 4 \times 2\sqrt{2} = 32\sqrt{2} \text{ cm}^2$$

**5.** Find the area of a parallelogram given in the figure. Also find the length of the altitude from vertex A on the side DC.

**Sol.** Area of parallelogram ABCD = 2 (Area of  $\triangle$ BCD) ... (1) Now, the sides of  $\triangle$ BCD are

a = 12 cm, b = 17 cm. and c = 25 cm.





From equation (1), we get

Area of parallelogram ABCD =  $2 \times 90 = 180 \text{ cm}^2$ 

Let the altitude of parallelogram be *h*.

Also, area of parallelogram  $ABCD = Base \times Altitude$ 

$$\Rightarrow$$
 180 = DC × h

$$\Rightarrow$$
 180 = 12 × h

 $\Rightarrow \qquad h = \frac{180}{12} = 15 \text{ cm}$ 

Hence, the area of parallelogram is  $180 \text{ cm}^2$  and the length of altitude is 15 cm.

- 6. A field in the form of parallelogram has sides 60 m and 40 m and one of its diagonals is 80 m long. Find the area of parallelogram.
- Sol. Let the field be ABCD.



Area of parallelogram ABCD =  $2 \times 1161.895 = 2323.79 \text{ m}^2$ 

- 7. The perimeter of a triangular field is 420 m and its sides are in the ratio 6 : 7 : 8. Find the area of the triangular field.
- **Sol.** Suppose that the sides in metres are 6x, 7x and 8x. Now 6r + 7r + 8r = Perimeter = 420

Now, 
$$6x + 7x + 8x - Perimeter - 420$$
  
⇒  $21x = 420$   
⇒  $x = \frac{420}{21}$   
⇒  $x = 20$   
∴ The sides of the triangular field are 6 × 20 m, 7 × 20 m, 8 × 20 m, *i.e.*, 120 m, 140 m, and 160 m.  
Now,  $s =$  Half the perimeter of triangular field  
 $= \frac{1}{2} \times 420 \text{ m} = 210 \text{ m}$ 

Using Heron's formula,

Area of the triangular field = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
  
=  $\sqrt{210(210-120)(210-140)(210-160)}$ 

i.e.,

$$= \sqrt{210 \times 90 \times 70 \times 50}$$
  
=  $\sqrt{66150000} = 8133.265 \text{ m}^2$ 

Hence, the area of the triangular field =  $8133.265 \text{ m}^2$ .

- 8. The sides of a quadrilateral ABCD are 6 cm, 8 cm, 12 cm and 14 cm (taken in order) respectively, and the angle between the first two sides is a right angle. Find its area.
- Sol. We have to find the area of quadrilateral ABCD. ABC is a right triangle.
  - : By Pythagoras theorem, we have



9. A rhombus shaped sheet with perimeter 40 cm and one diagonal 12 cm, is painted on both sides at the rate of ₹ 5 per cm<sup>2</sup>. Find the cost of painting.



$$= \frac{1}{2} \times 19 \text{ m} \times 12 \text{ m} = \frac{1}{2} \times 228 \text{ m}^2 = 114 \text{ m}^2$$

- 1. How much paper of each shade is needed to make a kite a kite given in the figure, in which ABCD is a square with diagonal 44 cm?
- **Sol.** Each diagonal of square = 44 cm and as B diagonals of a square bisect each other at right angles

:. Area of square ABCD  
= 
$$2(\text{area of } \Delta ABC)$$

$$=2(\frac{1}{2} \times 44 \times 22) = 2(44 \times 11)$$
  
= 968 cm<sup>2</sup>

... Paper of Red shade needed to make the kite

 $= \frac{1}{4} (968 \,\mathrm{cm}^2) = 242 \,\mathrm{cm}^2$ 

Paper of yellow shade needed to make the kite

 $= (242 + 242) \text{ cm}^2 = 484 \text{ cm}^2$ 

Let us find the area of a triangle with sides 20 cm, 20 cm and 14 cm which is at the bottom of the square ABCD. Now, semiperimeter

$$s = \frac{20 + 20 + 14}{2} = \frac{54}{2} = 27 \text{ cm}$$
Area of  $\Delta = \sqrt{s(s-a)(s-b)(s-c)}$ 

$$= \sqrt{27(27 - 20)(27 - 20)(27 - 14)}$$

$$= \sqrt{27 \times 7 \times 7 \times 13} = 21\sqrt{39}$$

$$= 21 \times 6.245 = 131.15 \text{ cm}^2$$

Paper of Green shade needed to make the kite

 $=(242 + 131.15) \text{ cm}^2 = 373.15 \text{ cm}^2$ 

- **2.** The perimeter of a triangle is 50 cm. One side of a triangle is 4 cm longer than the smaller side and the third side is 6 cm less than twice the smaller side. Find the area of the triangle.
- Sol. Let the smaller side of the triangle be x cm. Therefore, the second side will be (x + 4) cm, and third side is (2x 6) cm. Now, perimeter of triangle = x + (x + 4) + (2x - 6)

ow, perimeter of triangle = 
$$x + (x + 4) + (2x - 6)$$
  
=  $(4x - 2)$  cm



 $\Rightarrow$ 

Also, perimeter of triangle = 50 cm.  $4x = 52; x = 52 \div 4 = 13$ Therefore, the three sides are 13 cm, 17 cm, 20 cm

$$s = \frac{13 + 17 + 20}{2} = \frac{50}{2} = 25 \text{ cm}$$
  

$$\therefore \quad \text{Area of } \Delta = \sqrt{25(25 - 13)(25 - 17)(25 - 20)}$$
  

$$= \sqrt{25 \times 12 \times 8 \times 5} = \sqrt{5 \times 5 \times 4 \times 3 \times 4 \times 2 \times 5}$$
  

$$= 5 \times 4 \times \sqrt{3 \times 2 \times 5} = 20\sqrt{30} \text{ cm}^2$$

**3.** The area of a trapezium is 475 cm<sup>2</sup> and height is 19 cm. Find the lengths of its two parallel sides if one side of 4 cm greater than the other.

Sol. Area of trapezium = 
$$\frac{1}{2} \times (\text{Sum of the parallel sides}) \times \text{height}$$
  
 $\Rightarrow 475 = \frac{1}{2} \times (x + x + 4) \times 19 \text{ cm}$   
 $\Rightarrow 2x + 4 = \frac{950}{19} = 50$ 

$$2x = 50 - 4 = 46$$
;  $x = 46 \div 2 = 23$ 

Hence, the length of two parallel sides are 23cm and (23 + 4) cm i.e 23 cm and 27 cm.

- **4.** A rectangular plot is given for constructing a house, having a measurement of 40 m long and 15 m in front. According to the laws, a minimum of 3 m, wide space should be left in the front and back each, 2 m wide space on each of other sides. Find the largest area where house can be constructed.
- Sol. The length of the rectangular plot = 40 m and the breadth of the plot = 15 m.As a minimum of 3 m wide space should be left in the front and back 2 m wide space each of other side, so the largest area where the house can be constructed

= [40-2(3)] [15-2(2)] = 34 × 11 = 374 m<sup>2</sup>

- 5. A field in the shape of a trapezium having parallel sides 90 m and 30 m These sides meet the third side at right angles. The length of the fourth side is 100 m. If it costs ₹ 4 to plough 1 m<sup>2</sup> of the field, find the total cost of ploughing the field.
- Sol. The two parallel sides are AB = 90 m and CD = 30 m.  $DM \perp AB$ Now, MB = AB - AM = 90 m - 30 m = 60 m.



$$= \frac{1}{2} \times 120 \times 80 = 4800 \,\mathrm{m}^2$$

Total cost of ploughing the field at the rate of  $\mathbf{\overline{\xi}} 4$  per m<sup>2</sup> =  $\mathbf{\overline{\xi}} (4800 \times 4)$  =  $\mathbf{\overline{\xi}} 19,200$ .

- 6. In given figure,  $\triangle ABC$  has sides AB = 7.5 cm, AC = 6.5 cm and BC = 7 cm. On base BC a parallelogram DBCE of same area as that of  $\triangle ABC$  is constructed. Find the height DF of the parallelogram.
- Sol. Sides of triangle ABC are 7.5 cm, 7cm and 6.5 cm. The semi-perimeter of  $\triangle$ ABC



$$s = \frac{7.5 + 7 + 6.5}{2} = \frac{21}{2} = 10.5 \text{ cm}$$
Area of  $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$ 

$$= \sqrt{10.5(10.5 - 7.5)(10.5 - 7)(10.5 - 6.5)}$$

$$= \sqrt{10.5 \times 3 \times 3.5 \times 4} = \sqrt{31.5 \times 14}$$

$$= \sqrt{441} = 21 \text{ cm}^2$$

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Now, as on base BC a parallelogram DBCE of same area as that of  $\triangle$ ABC is constructed. Therefore, area of || gm. DBCE = 21 cm<sup>2</sup> Also, area of || gm  $\triangle$ BCE = BC × DF

$$\begin{array}{rcl} \therefore & BC \times DF &=& 21 \ cm^2 \\ \Rightarrow & 7 \times DF &=& 21 \ cm^2 \\ \Rightarrow & DF &=& 21 \ cm^2 \div 7 \ cm &= 3 \ cm \end{array}$$

Hence, the height DF of the parallelogram = 3 cm.

7. The dimensions of a rectangle ABCD are 51 cm  $\times$  25 cm. A trapezium with its parallel sides QC and PD in the ratio 9 : 8, is cut off form the rectangle as shown in the given figure. If the area of the trapezium PQCD

is 
$$\frac{5}{6}$$
 th part of the area of the rectangle, find the lengths QC and PD.



Sol. ABCD is a rectangle in which AB = 51cm and BC = 25cm. Since parallel sides QC and PD are in the ratio 9 : 8, so let QC = 9x and PD = 8x.

Now, area of trapezium PQCD =  $\frac{1}{2} \times (9x + 8x) \times 25 \text{ cm}^2$ 

$$=\frac{1}{2}\times 17x\times 25$$

Area of rectangle ABCD =  $BC \times CD = 51 \times 25$ 

It is given that area of trapezium PQCD =  $\frac{5}{6}$  × Area of rectangle ABCD.

$$\therefore \qquad \frac{1}{2} \times 17x \times 25 = \frac{5}{6} \times 51 \times 25$$
$$\Rightarrow \qquad x = \frac{5}{6} \times 51 \times 25 \times 2 \times \frac{1}{17 \times 25} = 5$$

Hence, the length  $QC = 9x = 9 \times 5 = 45$  cm. and the length  $PD = 8x = 8 \times 5 = 40$  cm.

8. A design is made on a rectangular tile of dimensions  $50 \text{ cm} \times 70 \text{ cm}$  as shown in the given figure. The design shows 8 triangles, each of sides 26 cm, 17 cm and 25 cm. Find the total area of the design and the remaining area of the tile.



**Sol.** Given, the dimensions of rectangular tile are  $50 \text{ cm} \times 70 \text{ cm}$  $\therefore$  Area of rectangular tile =  $50 \times 70 = 3500 \text{ cm}^2$ 

The sides of a design of one triangle be a = 25 cm, b = 17 cm and c = 26 cm.

$$s = \frac{a+b+c}{2}$$
$$= \frac{25+17+26}{2} = \frac{68}{2} = 34 \text{ cm}$$

:.

Area of 
$$\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$$
  
[By Heron's formula]  

$$= \sqrt{34 \times 9 \times 17 \times 8}$$

$$= \sqrt{17 \times 2 \times 3 \times 3 \times 17 \times 2 \times 2 \times 2}$$

$$= 17 \times 3 \times 2 \times 2$$

$$= 204 \text{ cm}^2$$

Hence, the total area of the design is  $1632 \text{ cm}^2$  and the remaining area of the tile is  $1868 \text{ cm}^2$ .