

## NCERT Solutions for Class 11 Physics Chapter 13 Kinetic Theory

**1. Estimate the fraction of molecular volume to the actual volume occupied by oxygen gas at STP. Take the diameter of an oxygen molecule to be 3 Å.**

**Solution:**

Diameter of an oxygen molecule,  $d = 3 \text{ \AA}$

Radius,  $r = d / 2$

$$r = 3 / 2 = 1.5 \text{ \AA} = 1.5 \times 10^{-8} \text{ cm}$$

Actual volume occupied by 1 mole of oxygen gas at STP =  $22400 \text{ cm}^3$

Molecular volume of oxygen gas,  $V = 4 / 3 \pi r^3 \cdot N$

Where,  $N$  is Avogadro's number =  $6.023 \times 10^{23}$  molecules/ mole

Hence,

$$V = 4 / 3 \times 3.14 \times (1.5 \times 10^{-8})^3 \times 6.023 \times 10^{23}$$

We get,

$$V = 8.51 \text{ cm}^3$$

Therefore, ratio of the molecular volume to the actual volume of oxygen =  $8.51 / 22400 = 3.8 \times 10^{-4}$

**2. Molar volume is the volume occupied by 1 mol of any (ideal) gas at standard temperature and pressure (STP: 1 atmospheric pressure, 0 °C). Show that it is 22.4 litres.**

**Solution:**

The ideal gas equation relating pressure ( $P$ ), volume ( $V$ ), and absolute temperature ( $T$ ) is given as:

$$PV = nRT$$

Where,  $R$  is the universal gas constant =  $8.314 \text{ J mol}^{-1}\text{K}^{-1}$

$n$  = Number of moles = 1

$T$  = Standard temperature = 273 K

$P$  = Standard pressure = 1 atm =  $1.013 \times 10^5 \text{ Nm}^{-2}$

Hence,

$$V = nRT / P$$

$$= 1 \times 8.314 \times 273 / 1.013 \times 10^5$$

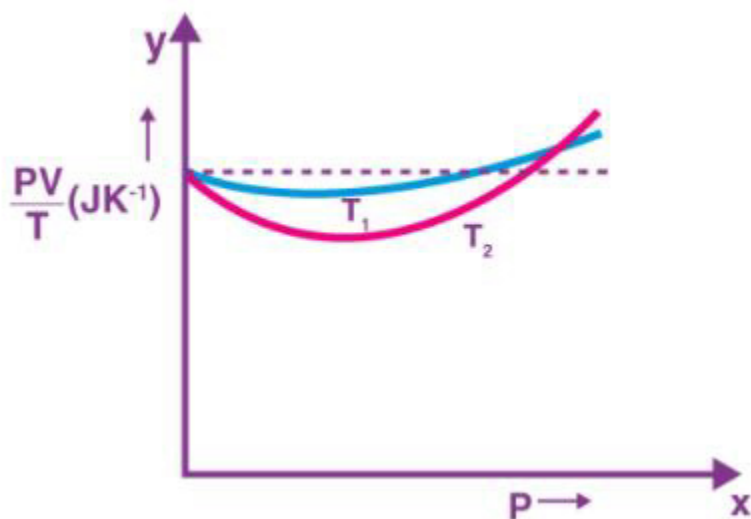
$$= 0.0224 \text{ m}^3$$

$$= 22.4 \text{ litres}$$

Therefore, the molar volume of a gas at STP is 22.4 litres

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3. Figure 13.8 shows plot of  $PV/T$  versus  $P$  for  $1.00 \times 10^{-3}$  kg of oxygen gas at two different temperatures.



(a) What does the dotted plot signify?

(b) Which is true:  $T_1 > T_2$  or  $T_1 < T_2$ ?

(c) What is the value of  $PV/T$  where the curves meet on the y-axis?

(d) If we obtained similar plots for  $1.00 \times 10^{-3}$  kg of hydrogen, would we get the same value of  $PV/T$  at the point where the curves meet on the y-axis? If not, what mass of hydrogen yields the same value of  $PV/T$  (for low pressure high temperature region of the plot)? (Molecular mass of  $H_2 = 2.02$  u, of  $O_2 = 32.0$  u,  $R = 8.31$  J  $mol^{-1}$   $K^{-1}$ .)

**Solution:**

(a) dotted plot is parallel to X-axis, signifying that  $nR$  [ $PV/T = nR$ ] is independent of  $P$ . Thus it is representing ideal gas behaviour

(b) the graph at temperature  $T_1$  is closer to ideal behaviour (because closer to dotted line) hence,  $T_1 > T_2$  (higher the temperature, ideal behaviour is the higher)

(c) use  $PV = nRT$

$$PV/T = nR$$

$$\text{Mass of the gas} = 1 \times 10^{-3} \text{ kg} = 1 \text{ g}$$

$$\text{Molecular mass of } O_2 = 32 \text{ g/mol}$$

Hence,

$$\begin{aligned} \text{Number of mole} &= \text{given weight} / \text{molecular weight} \\ &= 1/32 \end{aligned}$$

$$\text{So, } nR = 1/32 \times 8.314 = 0.26 \text{ J/K}$$

Hence,

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Value of  $PV / T = 0.26 \text{ J/ K}$

(d) 1 g of  $\text{H}_2$  doesn't represent the same number of mole

Eg. molecular mass of  $\text{H}_2 = 2 \text{ g/mol}$

Hence, number of moles of  $\text{H}_2$  require is  $1/32$  (as per the question)

Therefore,

Mass of  $\text{H}_2$  required = no. of mole of  $\text{H}_2$  x molecular mass of  $\text{H}_2$

$$= 1/32 \times 2$$

$$= 1/16 \text{ g}$$

$$= 0.0625 \text{ g}$$

$$= 6.3 \times 10^{-5} \text{ kg}$$

Hence,  $6.3 \times 10^{-5} \text{ kg}$  of  $\text{H}_2$  would yield the same value

**4. An oxygen cylinder of volume 30 litres has an initial gauge pressure of 15 atm and a temperature of  $27^\circ\text{C}$ . After some oxygen is withdrawn from the cylinder, the gauge pressure drops to 11 atm and its temperature drops to  $17^\circ\text{C}$ . Estimate the mass of oxygen taken out of the cylinder ( $R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$ , molecular mass of  $\text{O}_2 = 32 \text{ u}$ ).**

**Solution:**

Volume of gas,  $V_1 = 30 \text{ litres} = 30 \times 10^{-3} \text{ m}^3$

Gauge pressure,  $P_1 = 15 \text{ atm} = 15 \times 1.013 \times 10^5 \text{ Pa}$

Temperature,  $T_1 = 27^\circ\text{C} = 300 \text{ K}$

Universal gas constant,  $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$

Let the initial number of moles of oxygen gas in the cylinder be  $n_1$

The gas equation is given as follows:

$$P_1 V_1 = n_1 R T_1$$

Hence,

$$n_1 = P_1 V_1 / R T_1$$

$$= (15.195 \times 10^5 \times 30 \times 10^{-3}) / (8.314 \times 300)$$

$$= 18.276$$

But  $n_1 = m_1 / M$

Where,

$m_1$  = Initial mass of oxygen

$M$  = Molecular mass of oxygen = 32 g

Thus,

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$$m_1 = N_1 M = 18.276 \times 32 = 584.84 \text{ g}$$

After some oxygen is withdrawn from the cylinder, the pressure and temperature reduce.

$$\text{Volume, } V_2 = 30 \text{ litres} = 30 \times 10^{-3} \text{ m}^3$$

$$\text{Gauge pressure, } P_2 = 11 \text{ atm}$$

$$= 11 \times 1.013 \times 10^5 \text{ Pa}$$

$$\text{Temperature, } T_2 = 17^\circ \text{C} = 290 \text{ K}$$

Let  $n_2$  be the number of moles of oxygen left in the cylinder

The gas equation is given as:

$$P_2 V_2 = n_2 R T_2$$

Hence,

$$n_2 = P_2 V_2 / R T_2$$

$$= (11.143 \times 10^5 \times 30 \times 10^{-3}) / (8.314 \times 290)$$

$$= 13.86$$

But

$$n_2 = m_2 / M$$

Where,

$m_2$  is the mass of oxygen remaining in the cylinder

Therefore,

$$m_2 = n_2 \times M = 13.86 \times 32 = 453.1 \text{ g}$$

The mass of oxygen taken out of the cylinder is given by the relation:

Initial mass of oxygen in the cylinder – Final mass of oxygen in the cylinder

$$= m_1 - m_2$$

$$= 584.84 \text{ g} - 453.1 \text{ g}$$

We get,

$$= 131.74 \text{ g}$$

$$= 0.131 \text{ kg}$$

Hence, 0.131 kg of oxygen is taken out of the cylinder

**5. An air bubble of volume  $1.0 \text{ cm}^3$  rises from the bottom of a lake 40 m deep at a temperature of  $12^\circ \text{C}$ . To what volume does it grow when it reaches the surface, which is at a temperature of  $35^\circ \text{C}$ ?**

**Solution:**

$$\text{Volume of the air bubble, } V_1 = 1.0 \text{ cm}^3$$

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$$= 1.0 \times 10^{-6} \text{ m}^3$$

Air bubble rises to height,  $d = 40 \text{ m}$

Temperature at a depth of 40 m,  $T_1 = 12^\circ \text{ C} = 285 \text{ K}$

Temperature at the surface of the lake,  $T_2 = 35^\circ \text{ C} = 308 \text{ K}$

The pressure on the surface of the lake:

$$P_2 = 1 \text{ atm} = 1 \times 1.013 \times 10^5 \text{ Pa}$$

The pressure at the depth of 40 m:

$$P_1 = 1 \text{ atm} + d\rho g$$

Where,

$\rho$  is the density of water =  $10^3 \text{ kg / m}^3$

$g$  is the acceleration due to gravity =  $9.8 \text{ m/s}^2$

Hence,

$$P_1 = 1.013 \times 10^5 + 40 \times 10^3 \times 9.8$$

We get,

$$= 493300 \text{ Pa}$$

We have

$$P_1 V_1 / T_1 = P_2 V_2 / T_2$$

Where,  $V_2$  is the volume of the air bubble when it reaches the surface

$$V_2 = P_1 V_1 T_2 / T_1 P_2$$

$$= 493300 \times 1 \times 10^{-6} \times 308 / (285 \times 1.013 \times 10^5)$$

We get,

$$= 5.263 \times 10^{-6} \text{ m}^3 \text{ or } 5.263 \text{ cm}^3$$

Hence, when the air bubble reaches the surface, its volume becomes  $5.263 \text{ cm}^3$

**6. Estimate the total number of air molecules (inclusive of oxygen, nitrogen, water vapour and other constituents) in a room of capacity  $25.0 \text{ m}^3$  at a temperature of  $27^\circ \text{ C}$  and  $1 \text{ atm}$  pressure.**

**Solution:**

Volume of the room,  $V = 25.0 \text{ m}^3$

Temperature of the room,  $T = 27^\circ \text{ C} = 300 \text{ K}$

Pressure in the room,  $P = 1 \text{ atm} = 1 \times 1.013 \times 10^5 \text{ Pa}$

The ideal gas equation relating pressure (P), Volume (V), and absolute temperature (T) can be written as:

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$$PV = (k_B NT)$$

Where,

$$k_B \text{ is Boltzmann constant} = (1.38 \times 10^{-23}) \text{ m}^2 \text{ kg s}^{-2} \text{ K}^{-1}$$

N is the number of air molecules in the room

Therefore,

$$N = (PV / k_B T)$$

$$= (1.013 \times 10^5 \times 25) / (1.38 \times 10^{-23} \times 300)$$

We get,

$$= 6.11 \times 10^{26} \text{ molecules}$$

Hence, the total number of air molecules in the given room is  $6.11 \times 10^{26}$

**7. Estimate the average thermal energy of a helium atom at**

**(i) room temperature (27 °C),**

**(ii) the temperature on the surface of the Sun (6000 K),**

**(iii) the temperature of 10 million kelvin (the typical core temperature in the case of a star).**

**Solution:**

(i) At room temperature,  $T = 27^\circ \text{C} = 300 \text{ K}$

$$\text{Average thermal energy} = (3 / 2) kT$$

Where,

$$k \text{ is the Boltzmann constant} = 1.38 \times 10^{-23} \text{ m}^2 \text{ kg s}^{-2} \text{ K}^{-1}$$

Hence,

$$(3 / 2) kT = (3 / 2) \times 1.38 \times 10^{-23} \times 300$$

On calculation, we get,

$$= 6.21 \times 10^{-21} \text{ J}$$

Therefore, the average thermal energy of a helium atom at room temperature of  $27^\circ \text{C}$  is  $6.21 \times 10^{-21} \text{ J}$

(ii) On the surface of the sun,  $T = 6000 \text{ K}$

$$\text{Average thermal energy} = (3 / 2) kT$$

$$= (3 / 2) \times 1.38 \times 10^{-23} \times 6000$$

We get,

$$= 1.241 \times 10^{-19} \text{ J}$$

Therefore, the average thermal energy of a helium atom on the surface of the sun is  $1.241 \times 10^{-19} \text{ J}$

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(iii) At temperature,  $T = 10^7$  K

Average thermal energy =  $(3 / 2) kT$

$$= (3 / 2) \times 1.38 \times 10^{-23} \times 10^7$$

We get,

$$= 2.07 \times 10^{-16} \text{ J}$$

Therefore, the average thermal energy of a helium atom at the core of a star is  $2.07 \times 10^{-16}$  J

**8. Three vessels of equal capacity have gases at the same temperature and pressure. The first vessel contains neon (monatomic), the second contains chlorine (diatomic), and the third contains uranium hexafluoride (polyatomic). Do the vessels contain equal number of respective molecules? Is the root mean square speed of molecules the same in the three cases? If not, in which case is  $V_{\text{rms}}$  the largest?**

**Solution:**

All the three vessels have the same capacity, they have the same volume.

So, each gas has the same pressure, volume and temperature

According to Avogadro's law, the three vessels will contain an equal number of the respective molecules.

This number is equal to Avogadro's number,  $N = 6.023 \times 10^{23}$ .

The root mean square speed ( $V_{\text{rms}}$ ) of a gas of mass  $m$  and temperature  $T$  is given by the relation:

$$V_{\text{rms}} = \sqrt{3kT / m}$$

Where,

$k$  is Boltzmann constant

For the given gases,  $k$  and  $T$  are constants

Therefore,  $V_{\text{rms}}$  depends only on the mass of the atoms, i.e.,  $V_{\text{rms}} \propto (1/m)^{1/2}$

Hence, the root mean square speed of the molecules in the three cases is not the same.

Among neon, chlorine and uranium hexafluoride, the mass of neon is the smallest.

Therefore, neon has the largest root mean square speed among the given gases.

**9. At what temperature is the root mean square speed of an atom in an argon gas cylinder equal to the rms speed of a helium gas atom at  $-20^\circ\text{C}$ ? (atomic mass of Ar = 39.9 u, of He = 4.0 u).**

**Solution:**

Given

Temperature of the helium atom,  $T_{\text{He}} = -20^\circ\text{C} = 253 \text{ K}$

Atomic mass of argon,  $M_{\text{Ar}} = 39.9 \text{ u}$

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Atomic mass of helium,  $M_{\text{He}} = 4.0 \text{ u}$

Let  $(V_{\text{rms}})_{\text{Ar}}$  be the rms speed of argon and

Let  $(V_{\text{rms}})_{\text{He}}$  be the rms speed of helium

The rms speed of argon is given by:

$$(V_{\text{rms}})_{\text{Ar}} = \sqrt{3RT_{\text{Ar}} / M_{\text{Ar}}} \dots\dots\dots (i)$$

Where,

R is the universal gas constant

$T_{\text{Ar}}$  is temperature of argon gas

The rms speed of helium is given by:

$$(V_{\text{rms}})_{\text{He}} = \sqrt{3RT_{\text{He}} / M_{\text{He}}} \dots\dots\dots (ii)$$

Given that,

$$(V_{\text{rms}})_{\text{Ar}} = (V_{\text{rms}})_{\text{He}}$$

$$\sqrt{3RT_{\text{Ar}} / M_{\text{Ar}}} = \sqrt{3RT_{\text{He}} / M_{\text{He}}}$$

$$T_{\text{Ar}} / M_{\text{Ar}} = T_{\text{He}} / M_{\text{He}}$$

$$T_{\text{Ar}} = T_{\text{He}} / M_{\text{He}} \times M_{\text{Ar}}$$

$$= (253 / 4) \times 39.9$$

We get,

$$= 2523.675$$

$$= 2.52 \times 10^3 \text{ K}$$

Hence, the temperature of the argon atom is  $2.52 \times 10^3 \text{ K}$

**10. Estimate the mean free path and collision frequency of a nitrogen molecule in a cylinder containing nitrogen at 2.0 atm and temperature  $17^\circ \text{C}$ . Take the radius of a nitrogen molecule to be roughly  $1.0 \text{ \AA}$ . Compare the collision time with the time the molecule moves freely between two successive collisions (Molecular mass of  $\text{N}_2 = 28.0 \text{ u}$ ).**

**Solution:**

$$\text{Mean free path} = 1.11 \times 10^{-7} \text{ m}$$

$$\text{Collision frequency} = 4.58 \times 10^9 \text{ s}^{-1}$$

$$\text{Successive collision time} \cong 500 \times (\text{Collision time})$$

$$\text{Pressure inside the cylinder containing nitrogen, } P = 2.0 \text{ atm} = 2.026 \times 10^5 \text{ Pa}$$

$$\text{Temperature inside the cylinder, } T = 17^\circ \text{C} = 290 \text{ K}$$

$$\text{Radius of a nitrogen molecule, } r = 1.0 \text{ \AA} = 1 \times 10^{-10} \text{ m}$$

$$\text{Diameter, } d = 2 \times 1 \times 10^{-10} = 2 \times 10^{-10} \text{ m}$$



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Molecular mass of nitrogen,  $M = 28.0 \text{ g} = 28 \times 10^{-3} \text{ kg}$

The root mean square speed of nitrogen is given by the relation:

$$V_{\text{rms}} = \sqrt{3RT / M}$$

Where,

R is the universal gas constant =  $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$

Hence,

$$V_{\text{rms}} = 3 \times 8.314 \times 290 / 28 \times 10^{-3}$$

On calculation, we get,

$$= 508.26 \text{ m/s}$$

The mean free path ( $l$ ) is given by relation:

$$l = kT / \sqrt{2} \times \pi \times d^2 \times P$$

Where,

k is the Boltzmann constant =  $1.38 \times 10^{-23} \text{ kg m}^2 \text{ s}^{-2} \text{ K}^{-1}$

Hence,

$$l = (1.38 \times 10^{-23} \times 290) / (\sqrt{2} \times 3.14 \times (2 \times 10^{-10})^2 \times 2.026 \times 10^5)$$

We get,

$$= 1.11 \times 10^{-7} \text{ m}$$

Collision frequency =  $V_{\text{rms}} / l$

$$= 508.26 / 1.11 \times 10^{-7}$$

On calculation, we get,

$$= 4.58 \times 10^9 \text{ s}^{-1}$$

Collision time is given as:

$$T = d / V_{\text{rms}}$$

$$= 2 \times 10^{-10} / 508.26$$

On further calculation, we get

$$= 3.93 \times 10^{-13} \text{ s}$$

Time taken between successive collisions:

$$T' = l / V_{\text{rms}} = 1.11 \times 10^{-7} / 508.26$$

We get,

$$= 2.18 \times 10^{-10}$$

Hence,

$$T' / T = 2.18 \times 10^{-10} / 3.93 \times 10^{-13}$$

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On calculation, we get,

$$= 500$$

Therefore, the time taken between successive collisions is 500 times the time taken for a collision

**11. A metre long narrow bore held horizontally (and closed at one end) contains a 76 cm long mercury thread, which traps a 15 cm column of air. What happens if the tube is held vertically with the open end at the bottom?**

**Solution:**

Length of the narrow bore,  $L = 1 \text{ m} = 100 \text{ cm}$

Length of the mercury thread,  $l = 76 \text{ cm}$

Length of the air column between mercury and the closed end,  $l_a = 15 \text{ cm}$

Since the bore is held vertically in air with the open end at the bottom, the mercury length that occupies the air space is:

$$= 100 - (76 + 15)$$

$$= 9 \text{ cm}$$

Therefore,

The total length of the air column  $= 15 + 9 = 24 \text{ cm}$

Let  $h \text{ cm}$  of mercury flow out as a result of atmospheric pressure

So,

Length of the air column in the bore  $= 24 + h \text{ cm}$

And,

Length of the mercury column  $= 76 - h \text{ cm}$

Initial pressure,  $V_1 = 15 \text{ cm}^3$

Final pressure,  $P_2 = 76 - (76 - h)$

$= h \text{ cm}$  of mercury

Final volume,  $V_2 = (24 + h) \text{ cm}^3$

Temperature remains constant throughout the process

Therefore,

$$P_1 V_1 = P_2 V_2$$

On substituting, we get,

$$76 \times 15 = h (24 + h)$$

$$h^2 + 24h - 1140 = 0$$

On solving further, we get,

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$$= 23.8 \text{ cm or } -47.8 \text{ cm}$$

Since height cannot be negative. Hence, 23.8 cm of mercury will flow out from the bore

$$\text{Length of the air column} = 24 + 23.8 = 47.8 \text{ cm}$$

**12. From a certain apparatus, the diffusion rate of hydrogen has an average value of  $28.7 \text{ cm}^3 \text{ s}^{-1}$ . The diffusion of another gas under the same conditions is measured to have an average rate of  $7.2 \text{ cm}^3 \text{ s}^{-1}$ . Identify the gas.**

**[Hint: Use Graham's law of diffusion:  $R_1/R_2 = (M_2/M_1)^{1/2}$ , where  $R_1, R_2$  are diffusion rates of gases 1 and 2, and  $M_1$  and  $M_2$  their respective molecular masses. The law is a simple consequence of kinetic theory.]**

**Solution:**

Given

$$\text{Rate of diffusion of hydrogen, } R_1 = 28.7 \text{ cm}^3\text{s}^{-1}$$

$$\text{Rate of diffusion of another gas, } R_2 = 7.2 \text{ cm}^3\text{s}^{-1}$$

According to Graham's Law of diffusion,

We have,

$$R_1 / R_2 = \sqrt{M_2 / M_1}$$

Where,

$M_1$  is the molecular mass of hydrogen = 2.020g

$M_2$  is the molecular mass of the unknown gas

Hence,

$$\begin{aligned} M_2 &= M_1 (R_1 / R_2)^2 \\ &= 2.02 (28.7 / 7.2)^2 \end{aligned}$$

We get,

$$= 32.09 \text{ g}$$

32 g is the molecular mass of oxygen.

Therefore, the unknown gas is oxygen.

**13. A gas in equilibrium has uniform density and pressure throughout its volume. This is strictly true only if there are no external influences. A gas column under gravity, for example, does not have a uniform density (and pressure). As you might expect, its density decreases with height. The precise dependence is given by the so-called law of atmospheres**

$$n_2 = n_1 \exp [ -mg (h_2 - h_1) / k_B T ]$$

where  $n_2, n_1$  refer to number density at heights  $h_2$  and  $h_1$  respectively. Use this relation to derive the equation for sedimentation equilibrium of a suspension in a liquid column:

$$n_2 = n_1 \exp [ -mg N_A (\rho - \rho') (h_2 - h_1) / (\rho RT) ]$$

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where  $\rho$  is the density of the suspended particle, and  $\rho'$ , that of surrounding medium. [ $N_A$  is Avogadro's number, and  $R$  the universal gas constant.] [Hint : Use Archimedes principle to find the apparent weight of the suspended particle.]

**Solution:**

Law of atmosphere

$$n_2 = n_1 \exp [ -mg (h_2 - h_1) / k_B T ] \text{ ———(1)}$$

The suspended particle experiences an apparent weight because of the liquid displaced

According to Archimedes principle

Apparent weight = Weight of the water displaced – weight of the suspended particle

$$= mg - m'g$$

$$= mg - V\rho'g = mg - (m/\rho) \rho'g$$

$$= mg (1 - (\rho'/\rho)) \text{ ———(2)}$$

$\rho'$  = Density of the water

$\rho$  = Density of the suspended particle

$m'$  = Mass of the suspended particle

$m$  = Mass of the water displaced

$V$  = Volume of a suspended particle

$$\text{Boltzmann's constant (K)} = R/N_A \text{ ———(3)}$$

Substituting equation (2) and equation (3) in equation (1)

$$n_2 = n_1 \exp [ -mg (h_2 - h_1) / k_B T ]$$

$$n_2 = n_1 \exp [ -mg (1 - \rho'/\rho) (h_2 - h_1) N_A / (RT) ]$$

$$n_2 = n_1 \exp [ -mg N_A (\rho - \rho') (h_2 - h_1) / (\rho RT) ]$$

**14. Given below are densities of some solids and liquids. Give rough estimates of the size of their atoms :**

Substance	Atomic Mass (u)	Density ( $10^3$ Kg m <sup>-3</sup> )
Carbon (diamond)	12.01	2.22
Gold	197.00	19.32
Nitrogen (liquid)	14.01	1.00
Lithium	6.94	0.53
Fluorine (liquid)	19.00	1.14

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[Hint: Assume the atoms to be 'tightly packed' in a solid or liquid phase, and use the known value of Avogadro's number. You should, however, not take the actual numbers you obtain for various atomic sizes too literally. Because of the crudeness of the tight packing approximation, the results only indicate that atomic sizes are in the range of a few Å].

**Solution:**

If  $r$  is the radius of the atom then the volume of each atom =  $(4/3)\pi r^3$

Volume of all the substance =  $(4/3)\pi r^3 \times N = M/\rho$

$M$  is the atomic mass of the substance

$\rho$  is the density of the substance

One mole of the substance has  $6.023 \times 10^{23}$  atoms

$$r = (3M/4\pi\rho \times 6.023 \times 10^{23})^{1/3}$$

For carbon,  $M = 12.01 \times 10^{-3}$  kg and  $\rho = 2.22 \times 10^3$  kg m<sup>-3</sup>

$$\begin{aligned} R &= (3 \times 12.01 \times 10^{-3}/4 \times 3.14 \times 2.22 \times 10^3 \times 6.023 \times 10^{23})^{1/3} \\ &= (36.03 \times 10^{-3}/167.94 \times 10^{26})^{1/3} \end{aligned}$$

$$1.29 \times 10^{-10} \text{ m} = 1.29 \text{ \AA}$$

For gold,  $M = 197 \times 10^{-3}$  kg and  $\rho = 19.32 \times 10^3$  kg m<sup>-3</sup>

$$\begin{aligned} R &= (3 \times 197 \times 10^{-3}/4 \times 3.14 \times 19.32 \times 10^3 \times 6.023 \times 10^{23})^{1/3} \\ &= 1.59 \times 10^{-10} \text{ m} = 1.59 \text{ \AA} \end{aligned}$$

For lithium,  $M = 6.94 \times 10^{-3}$  kg and  $\rho = 0.53 \times 10^3$  kg/m<sup>3</sup>

$$\begin{aligned} R &= (3 \times 6.94 \times 10^{-3}/4 \times 3.14 \times 0.53 \times 10^3 \times 6.023 \times 10^{23})^{1/3} \\ &= 1.73 \times 10^{-10} \text{ m} = 1.73 \text{ \AA} \end{aligned}$$

For nitrogen (liquid),  $M = 14.01 \times 10^{-3}$  kg and  $\rho = 1.00 \times 10^3$  kg/m<sup>3</sup>

$$\begin{aligned} R &= (3 \times 14.01 \times 10^{-3}/4 \times 3.14 \times 1.00 \times 10^3 \times 6.023 \times 10^{23})^{1/3} \\ &= 1.77 \times 10^{-10} \text{ m} = 1.77 \text{ \AA} \end{aligned}$$

For fluorine (liquid),  $M = 19.00 \times 10^{-3}$  kg and  $\rho = 1.14 \times 10^3$  kg/m<sup>3</sup>

$$\begin{aligned} R &= (3 \times 19 \times 10^{-3}/4 \times 3.14 \times 1.14 \times 10^3 \times 6.023 \times 10^{23})^{1/3} \\ &= 1.88 \times 10^{-10} \text{ m} = 1.88 \text{ \AA} \end{aligned}$$